

WEEK #1 – HEAT TRANSFER

Topics

Fourier's law and applications (temperature-dependent thermal conductivity, shear heating)

Steady-state spherical heat conduction (in a shell, with advection, with heat production)

Time-dependent heat conduction (Stefan problem, thermal inertia)

Heating during accretion

Numerical approaches

Equations

$$F = -k \frac{dT}{dz} \quad \frac{DT}{Dt} = \frac{\partial T}{\partial t} + u \cdot \nabla T = \kappa \nabla^2 T + \frac{H}{\rho C_p} \quad t \sim d^2/\kappa$$

Numbers

$$k \sim 3 \text{ W m}^{-1} \text{ K}^{-1} \quad \kappa \sim 10^{-6} \text{ m}^2 \text{ s}^{-1} \quad H \sim 3 \times 10^{-12} \text{ W kg}^{-1} \text{ (Earth, present-day)}$$

²⁶Al decay: 3 MeV per atom, $t_{1/2} \sim 0.7$ Myr

$C_p \sim 1 \text{ kJ kg}^{-1} \text{ K}^{-1}$ (rock) $\sim 2 \text{ kJ kg}^{-1} \text{ K}^{-1}$ (ice), $L \sim 0.3 \text{ MJ kg}^{-1}$ (rock/ice)

References

Turcotte, D.L., G. Schubert, *Geodynamics*, 2nd ed., CUP 2002, Chapter 4.

Carslaw, H.S., J.C. Jaeger, *Conduction of Heat in Solids*, 2nd ed., OUP 1959, all of it esp. Ch 9.

O'Reilly, T.C., G.F. Davies, Magma transport of heat on Io – a mechanism allowing a thick lithosphere, *Geophys. Res. Lett.* 8, 313-316, 1981.