



2 A geological fingerprint of low-viscosity fault fluids mobilized 3 during an earthquake

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6 [1] The absolute value of stress on a fault during slip is a critical unknown quantity in
7 earthquake physics. One of the reasons for the uncertainty is a lack of geological
8 constraints in real faults. Here we calculate the slip rate and stress on an ancient fault
9 in a new way based on rocks preserved in an unusual exposure. The study area consists of
10 a fault core on Kodiak Island that has a series of asymmetrical intrusions of ultrafine-
11 grained fault rock into the surrounding cataclasite. The intrusive structures have ductile
12 textures and emanate upward from a low-density layer. We interpret the intrusions as
13 products of a gravitational (Rayleigh-Taylor) instability where the spacing between
14 intrusions reflects the preferred wavelength of the flow. The spacing between intrusions is
15 1.4 ± 0.5 times the thickness of the layer. This low spacing-to-thickness ratio cannot be
16 explained by a low Reynolds number flow but can be generated by one with moderate
17 Reynolds numbers. Using a range of density contrasts and the geometry of the outcrop
18 as constraints, we find that the distance between intrusions is best explained by moderately
19 inertial flow with fluid velocities on the order of 10 cm/s. The angle that the intrusions
20 are bent over implies that the horizontal slip velocity was comparable to the vertical rise
21 velocity, and therefore, the fault was slipping at a speed of order 10 cm/s during
22 emplacement. These slip velocities are typical of an earthquake or its immediate afterslip
23 and thus require a coseismic origin. The Reynolds number of the buoyant flow requires a
24 low viscous stress of at most 20 Pa during an earthquake.

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28 1. Introduction

29 [2] In order to successfully model the initiation, propa-
30 gation or arrest of an earthquake, quantitative measures of
31 the absolute resisting stresses on faults are necessary.
32 Unfortunately, these stresses are still uncertain. Seismology
33 alone cannot measure absolute stresses [Abercrombie *et al.*,
34 2006]. Rock mechanics suggests that the absolute stress
35 between two solid rocks should be on the order of the
36 lithostatic stress [Byerlee, 1970]. However, heat flow
37 studies fail to measure the implied frictional heating
38 [Lachenbruch and Sass, 1980, 1992]. Furthermore, recent
39 laboratory and theoretical work suggests that qualitatively
40 different processes are active at high slip rates that funda-
41 mentally change the resisting stresses [Andrews, 2002;
42 Brodsky and Kanamori, 2001; Fialko and Khazan, 2005;
43 Nielsen *et al.*, 2008; Rice, 2006; Spray, 2005; Yuan and
44 Prakash, 2008]. Ground truth for these proposals is limited
45 because there are few tools to determine the slip rate of
46 ancient faults and almost no recognized record of the
47 seismic stresses [Cowan, 1999].

[3] Here we present observations and analysis of an 48
unusual site that can help constrain the local absolute 49
stresses on a fault. The faulting preserved at the key outcrop 50
occurred at 12–14 km depth in a megathrust in an accre- 51
tionary prism that is now exposed on Kodiak Island, Alaska 52
[Rowe *et al.*, 2005; Rowe, 2007]. The fault core is composed 53
of a ~ 3.5 cm layer of ultrafine-grained black rock that is 54
embedded in a 13.5m-thick cataclasite that is interpreted as 55
a subduction thrust by Byrne [1984] (Figures 1 and 2). A 56
series of cusped intrusions that extend upward from the core 57
are interpreted as buoyant intrusions into the overlying 58
layer. Such gravitational (Raleigh-Taylor) instabilities are 59
general features of layered materials whenever a higher- 60
density layer overlies a lower density layer and both layers 61
behave ductilely. This study analyzes the spacing of the 62
intrusions using a fluid dynamic model in order to: (1) 63
determine the emplacement speed and thus provide a new 64
geological tool to identify seismogenic faults in the geolog- 65
ical record and (2) constrain the rheology and local stress on 66
the fault during emplacement. 67

[4] Ultrafine-grained fault rocks like the one studied here 68
have been the subject of intense scrutiny in previous work 69
[Sibson and Toy, 2006]. The major debate revolves around 70
whether or not the unit is a frictional melt (pseudotachylyte) 71
or an ultracataclasite [Di Toro *et al.*, 2005; Magloughlin and 72
Spray, 1992; Rowe *et al.*, 2005; Wenk *et al.*, 2000]. 73
Petrological and geochemical techniques are fast developing 74

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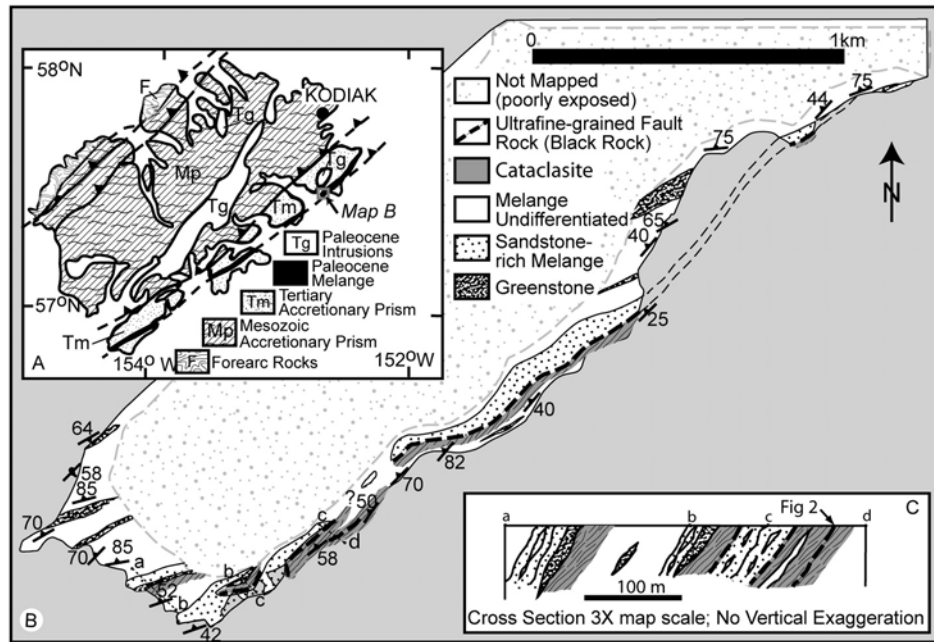


Figure 1. Geologic map of Pasagshak Peninsula showing location of ultrafine-grained fault rock, i.e., the “black rock” that is the subject of this paper. (a) Regional location map. (b) Map of Pasagshak Peninsula. Thickness of black rock is exaggerated to better show its location and its lateral extent of 2.5 km. (c) Cross-section. Note that black rock occurs in three layers; only the structurally lowest black rock layer is included in the associated cataclasite; the others occur at the boundary with sandstone beds. Surface datum for cross-section is sea level, and three separate subsections connect through equivalent structural positions along strike. The position of the photo in Figure 2 is marked on the cross-section in inset C. Figure modified from Rowe *et al.* [2005, Figure 1].

75 to resolve the issue [Lin, 2007]. Here we present an
 76 alternative approach. Rather than directly constraining the
 77 chemistry, temperature or mineralogy of the unit, we will
 78 instead measure its geometry to constrain the rheology. As
 79 will be discussed near the end of the paper, the rheology
 80 inferred from the flow analysis is consistent with either a
 81 granular flow or a frictional melt origin as suggested by
 82 previous work at this site [Meneghini *et al.*, 2007; Rowe *et*
 83 *al.*, 2005]. Therefore the new technique is complementary
 84 to the previously explored ones. In order to emphasize that
 85 no prior knowledge about the genesis of the unit is neces-
 86 sary for the flow analysis, we will postpone a discussion of
 87 the correct classification of the ultrafine-grained fault rock
 88 to the final section of this paper. For the bulk of the paper,
 89 we will keep the discussion general by simply referring to
 90 the ultrafine-grained fault rock as the “black rock.”

91 [5] This paper begins with the geological observations.
 92 After reviewing the geological context that is more fully
 93 documented elsewhere, we present the central observations
 94 of this paper: the intrusions at the Kodiak Island site. We
 95 will highlight the features indicative of ductile, buoyant
 96 behavior both by describing the outcrop and comparing it to
 97 similar structures formed by gravitational instabilities in
 98 sedimentary rocks. We will then proceed to interpret the
 99 spacing of the intrusions in terms of the fluid dynamics with
 100 the aid of a linear stability analysis. In order to explain the
 101 data, we will incrementally add complications to the model
 102 and ultimately conclude that nonnegligible inertia in the
 103 fluid is necessary. The analysis results in a constraint on
 104 the strain rate of the flow. Finally, we will determine the

velocity and stress at the time of intrusion and interpret 105
 these in terms of the rheologies of plausible materials in the 106
 fault. 107

2. Observations 108

2.1. Geological Context 109

[6] The Kodiak accretionary complex of Alaska is an 110
 exhumed subduction zone that has modern analogs locally 111
 offshore in the Eastern Aleutian Trench [Plafker *et al.*, 112
 1994]. Plate boundary thrust faults are preserved as mé- 113
 langes in several accreted units. These mélanges have been 114
 interpreted by previous workers as ancient decollements 115
 formed during subduction to ~12–14 km [Byrne, 1984; 116
 Vrolijk *et al.*, 1988]. The stratigraphic younging directions 117
 of the surrounding geological units indicate that the current 118
 upward direction preserves the original orientation [Rowe, 119
 2007]. 120

[7] Within one mélangé, four parallel, high-strain, strong- 121
 ly foliated cataclastic shear zones occur within a structural 122
 thickness of 300 m (Figure 1). Compositional data suggest 123
 that the cataclastic shear zones are derived from the sur- 124
 rounding mélangé but are differentiable from it in texture 125
 and thickness. The thickness of the of individual bands 126
 where measured was 31 m, 14 m, 25 m and 14 m in order 127
 from west to east (structurally downsection) across Figure 1. 128
 Cataclasites are composed of submillimeter to decimeter 129
 sandstone fragments in a matrix of fine-grained pelitic 130
 material. The cataclasites show a scaly foliation due to 131
 pressure solution superimposed on the cataclastic texture 132

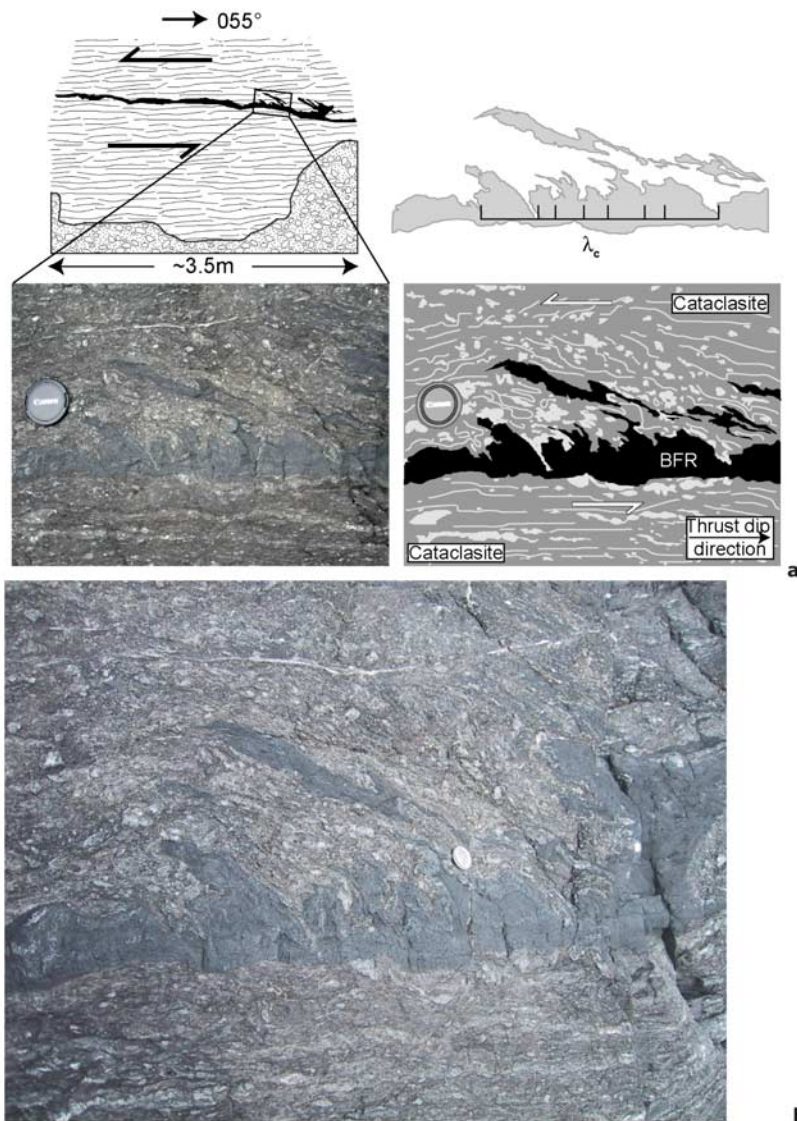


Figure 2. Photograph and explanatory sketch of the outcrop of black rock in Kodiak Island, AK. Lens cap diameter on bottom pictures is 6 cm for scale. (a) Upper left sketch shows general outcrop-scale appearance of black rock layer cutting at a low angle the cataclasite fabric (thin discontinuous lines mark structural fabric). Close-up view in lower photograph and sketch show ductile intrusions of black material in hanging wall cataclasite. Cataclasite fabric is locally disrupted around intrusions (see fabric around lens cap and compare it with subplanar fabric of lower cataclasite layer), suggesting that cataclasites were able to ductilely deform at time of intrusion and did not respond in a brittle manner to upward flow. Deflection of the intrusive structures due to shear consistent with thrust motion is also visible, especially in taller intrusions. Upper right inset illustrates only the intrusion geometry, showing the spacing between intrusions as measured on the outcrop. These intervals are used as proxies for wavelengths used in calculations. (b) Alternative angle on the same exposure showing that the isolated black rock patches on the far right in the photograph in Figure 2a are the distended peaks of more intrusions. Wavelengths can only be measured on the intrusions where the connection to the source layer is fully exposed. All 7 examples with sufficient exposure have been measured in Figure 2a and included in this paper.

133 [Rowe, 2007]. Within each shear zone, the cataclasite
 134 textures vary at field-scale in clast concentration, strength/
 135 style of foliation and degree of shearing [Rowe *et al.*, 2005].
 136 Textural domains can be bounded by either thin shear
 137 surfaces or have gradational relationships to one another.

138 [8] The cataclasite bands are interpreted as episodes of
 139 localized deformation in the decollement evolution and

are more fully documented by Rowe [2007]. They show that 140
 the paleodecollement was a series of anastomosing surfaces 141
 rather than repeated faulting on a single thrust surface 142
 [Rowe *et al.*, 2005]. On the basis of previous work on 143
 accretionary prism development, the simplest interpretation 144
 is progressive accretion by underplating at the base resulting 145
 in the structurally highest cataclasite being the oldest 146

147 [Sample and Fisher, 1986]. The order of individual cata-
 148 clasite band activity does not have any direct bearing on the
 149 interpretation here.

150 [9] Evidence of extreme strain localization in the cata-
 151 clastic fault zones manifests as decimeter-thick planar to
 152 irregular beds of dark gray to black ultrafine-grained fault
 153 rocks that cut and complexly intrude three of the cataclas-
 154 sites. The thickest cataclasite band contains no black rock.
 155 The black layers occur within the cataclasite or at the sharp
 156 boundary between the shear zone and a bounding 3–10 m
 157 thick massive sandstone unit from the mélange. The black
 158 rocks in the fault are exceptionally continuous for distances
 159 of more than 2.5 km in layers that are subparallel to the
 160 strike of the cataclasite bands (Figure 1).

161 [10] These black rock layers are distinguished in the field
 162 by hardness, black color and vitreous to earthy luster.
 163 Microscopy has confirmed that the black rock textures
 164 sharply contrast with those observed in the cataclasites.
 165 The black rocks have: (1) ultrafine grains ranging from 1 to
 166 10 microns, as opposed to the cataclasite grains ranging from
 167 the submillimeter scale to tens of centimeters, (2) subrounded
 168 quartz and plagioclase as opposed to rounded grains, (3) a
 169 matrix containing tabular euhedral, zoned plagioclase crys-
 170 tals as opposed to uniform anhedral plagioclase and (4) no
 171 preferred orientation of platy minerals at any scale, as
 172 opposed to scaly foliation [Meneghini *et al.*, 2008].

173 [11] The chemistry of the black rocks is consistent with
 174 being derived from the cataclasite. The major mineral con-
 175 stituents for both units are quartz, albite, chlorite and illite.
 176 The mean chemical composition of the two units is within
 177 the standard deviation of the measurements for all major
 178 elements except Na₂O (Table B1). This minor differences in
 179 bulk chemistry suggest minor fractionation between the
 180 cataclasite and the black rock, possibly due to incomplete
 181 melting [Meneghini *et al.*, 2007]. In particular, the ultrafine-
 182 grained matrix of the black rocks is slightly depleted in
 183 phyllosilicates and enriched in tabular albitic feldspar rela-
 184 tive to the cataclasites. However, the overall similarities
 185 indicate a close relationship between the units.

186 2.2. Black Rock Intrusions

187 [12] In one locality where the black rock is entirely
 188 embedded in the cataclasite, flame-like intrusions of black
 189 rock originate from the black rock layer and enter the upper
 190 cataclasite (Figure 2). Here the cataclasite is 14 m thick. The
 191 black rock is inside a 0.3 m thick sandstone clast-rich
 192 textural domain of the cataclasite.

193 [13] The intrusions taper with distance upward from the
 194 black rock and terminate within 0.1 m of the interface. The
 195 smoothly curved forms imply ductile deformation. Pointed
 196 cusps in ductile rocks are commonly interpreted as indica-
 197 tive of the relative viscosity of the two layers because the
 198 lower viscosity unit forms smaller angles as it is more easily
 199 deformed [Davis and Reynolds, 1996; Dieterich and Onat,
 200 1969]. In this case, the elongate tips of the black rock
 201 intrusions indicate that the black rock is less viscous than
 202 the overlying cataclasite.

203 [14] The base of the black layer is smooth with no
 204 intrusions extending downward from the layer. The vertical
 205 asymmetry suggests that the intrusions are buoyant features
 206 driven by a density contrast between the less dense black rock
 207 and the more dense upper cataclasite. To investigate whether

Table 1. Density Measurements^a

Unit	Mean (kg/m ³)	Standard Deviation (kg/m ³)	
Black rock—bulk	2685	19	t1.3
Cataclasite—bulk	2722	23	t1.4
Sandstone—bulk	2683	7	t1.5
Black rock—grain	2726	45	t1.6
Cataclasite—grain	2849	19	t1.7

^aReported values are the dry bulk density of eight cataclasite, seven black rock, and two sandstone samples and grain density on three powdered samples. We measured the volume of 1-in. core or sawed rectangular solid samples and the volume of powders with a Quantachrome gas comparison pycnometer. We determined mass with a scale sensitive to 10⁻⁶ kg. Up to four repeat measurements were performed on most samples with standard deviations of 0.5%.

the density difference between the units is significant, we
 measured the densities of the preserved rocks (Table 1). The
 grain density of the black rock is presently 5% less than the
 surrounding cataclasites. The difference is explained by a
 slight depletion of sheet silicate minerals in the black rock
 [Meneghini *et al.*, 2008]. The preserved porosity in the black
 rock is less than in the cataclasite, so the net density
 difference is now 1.4% with a standard deviation of 1.1%.

[15] Extrapolating the measured densities to emplacement
 conditions requires knowledge of the genesis of the black
 rock. We will derive a range of possible in situ density
 changes by considering two end-member candidates for
 generating the black rocks: melting and granular flow.
 Melting of the cataclasite composition reported in Appendix
 B in bulk and subsequent heating to 1400°C reduces the
 theoretical density by 20% relative to the preserved density as
 calculated with the thermodynamic MELTS model via the
 Conflow software [Mastin and Ghioroso, 2000]. Mobilized
 granular flow dilates via intergranular collisions. Under
 confined, high-pressure conditions, the maximum dilatation
 corresponds to the random-loose-packing of the grains. The
 most dispersed random-loose-packing function is that of
 monodispersed spheres which has a solid volume fraction
 of 55% [Song *et al.*, 2008]. If the grains are in this state and
 the intergranular region is filled with water with a density of
 1000 kg/m³, the density of the mixture is ~30% less than the
 bulk cataclasite. The actual expansion of a natural granular
 medium must be less than this extreme bound as the grains
 are neither spherical nor mono-dispersed. In summary, either
 situation (melting or granular flow) reduces the black rock
 density relative to the cataclasite and thus supports the
 inference of a buoyantly driven intrusion.

[16] The intrusive structures are sheared in a direction
 consistent with motion on the thrust as inferred by kine-
 matic indicators in the cataclasite and mélange (bending
 leftward in Figure 2) [Rowe, 2007]. The cross-section is
 within 10° of parallelism to the mean transport direction in
 the cataclasite. The taller intrusions, such as that in the
 center of Figure 2, are progressively inclined with increas-
 ing distance from the source layer of black rock, varying
 from 15° from vertical at the base to 68° at the crest. Above
 the contiguous intrusions, even longer features are stretched
 out to be coplanar with the fault surface. The shape
 indicates the intrusions were sheared at the same time as
 they grew vertically so that the points furthest from the fault
 surface accumulated the most shear.

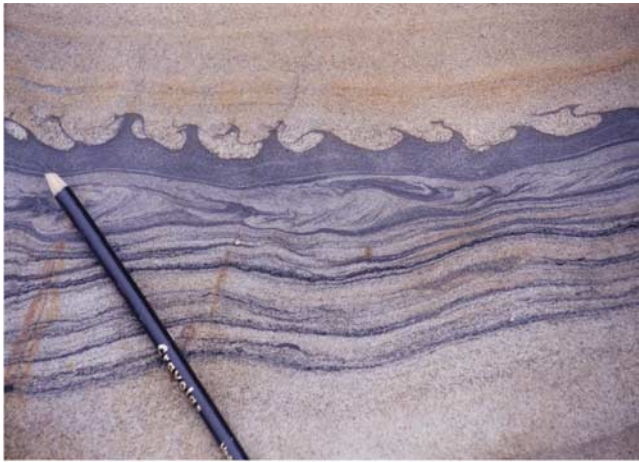


Figure 3. Sedimentary flame structures, Carmelo Formation, Pt. Lobos, California. Pencil diameter is 8 mm. Note systematic spacing and direction of deflection and intrusion perpendicularity to basal bedding contact.

254 [17] The deformation of the intrusions is gradational
 255 throughout the intrusive zone without any sign of relative
 256 overprinting or cross-cutting, so horizontal and vertical
 257 motions were simultaneous. The inclination of the eight
 258 measurable intrusive structures averaged over their entire
 259 heights is $38^\circ \pm 15^\circ$ from vertical and thus the horizontal
 260 and vertical velocities are comparable. Therefore, by con-
 261 straining the emplacement rate of the structures, we learn
 262 about the shear rate during their formation.

263 [18] Even though the overlying layer is stiffer than the
 264 black rock, flow occurred in the cataclasite to accommodate
 265 the growing intrusions. This deformation is recorded by the
 266 curvature of the otherwise planar fabric in the cataclasite
 267 between the intrusions (see the fabric between the lens cap
 268 and the black fault rock in Figure 2). The fabric stretches
 269 and bends so that it remains parallel to the curved black
 270 rock-cataclasite boundary between intrusions. The cataclas-
 271 tic fabric provides evidence that the intrusions spacing is not
 272 governed by post-emplacement layer-parallel shortening
 273 because the fabric is subparallel 0.3 m above and directly
 274 below the fault core.

275 [19] The ductile textures occur exclusively where granu-
 276 lar cataclasite overlies a horizon of black rock. Elsewhere,
 277 sandstone overlies the black rock and the black rock
 278 intrudes through brittle fractures. The presence of deforma-
 279 ble granular cataclasite appears to be required to generate
 280 the ductile intrusions.

281 [20] Individual intrusions are spaced closely together
 282 relative to the thickness of the layer. Over seven measurable
 283 intrusion intervals (tick marks in Figure 2), the spacing is
 284 4.7 ± 1.5 cm and the layer thickness is 3.5 ± 0.6 cm where
 285 the error ranges are 1 standard deviation. Spacing of the
 286 intrusions is measured between minima along a median line
 287 defined by the layer thickness away from the intrusions
 288 based on field measurements and analysis of photos from
 289 multiple angles to the outcrop. This regular spacing of the
 290 intrusions suggests instability at a preferred wavelength,
 291 which is a general feature of gravitationally unstable flows
 292 that will be discussed at length in subsequent sections.

[21] In summary, we infer from the geometry that the 293
 structures in Figure 2 are buoyant, ductile intrusion of the 294
 black rock into the overlying cataclasite. The black rock 295
 was less dense and less viscous than the cataclasite it 296
 intruded. The intrusion occurred simultaneously and at a 297
 similar strain rate to shear of the fault zone. 298
 299

2.3. Flame Structures: A Soft-Sediment Analog 299

[22] The geometry of the black rock intrusions is similar 300
 to flame structures that are observed in soft sediment 301
 [Ronnlund, 1989; Visher and Cunningham, 1981]. The 302
 analogy is instructive and helps to support the inferred 303
 buoyant origin of the intrusions. 304

[23] We next briefly review the soft-sediment analog and 305
 its similarities to the rocks observed here. 306

[24] Flame structures are a somewhat rare but distinctive 307
 structure known from soft sediment deformation [Allen, 308
 1982]. They occur in restricted localities where sand 309
 overlies mud along a sharp contact as in turbidites and a detailed 310
 description is given by Allen [1985]. The flame structures 311
 are the upward injections of mud into the sand layer that are 312
 generally found only on a restricted portion of an interface 313
 [Dasgupta, 1998]. 314

[25] The structures have been attributed to an instability 315
 of the sediments by many authors [Allen, 1982; Anketell et 316
 al., 1970; Brodzikowski and Haluszczak, 1987; Collinson, 317
 1994; Kelling and Walton, 1957; Lowe, 1975; Maltman, 318
 1994; Owen, 1987, 1996]. Most work suggests that the 319
 instability is gravitational because of an inverse gradation in 320
 bulk density [Allen, 1982; Collinson, 1994; Kelling and 321
 Walton, 1957; Lowe, 1975; Maltman, 1994; Owen, 1996]. 322
 The gravitational model that interprets the flames as buoy- 323
 ant intrusions best explains the experimental data and 324
 natural occurrence. 325

[26] Morphologically, flames show many characteristic 326
 features that require a viscous, two-fluid origin. Intrusion of 327
 mud is always perpendicular to layering, i.e., upward. The 328
 peaks of the flame structures have a characteristic spacing 329
 and are concave-upward, pinching out at some height. 330

[27] As the prevalence of planar-bedded turbidites dem- 331
 onstrates, the instability occurs only under special circum- 332
 stances when liquefaction is triggered by an external event, 333
 e.g., vibration from the passage of turbidity currents [Allen, 334
 1982] or shaking from earthquakes [Bhattacharya and 335
 Bandyopadhyay, 1998; Horváth et al., 2005]. It is common 336
 for flame structures to occur over only a limited area even 337
 when bedding surfaces continue over a greater extent 338
 [Dasgupta, 1998]. 339

[28] In an example from the Carmelo Formation turbid- 340
 ites at Pt. Lobos in central California, USA, flame struc- 341
 tures formed by upward injection of lighter, low-density 342
 mud into higher-density sands (Figure 3; for a detailed 343
 description of the sedimentological context see Clifton 344
 [1984] and Dasgupta [1998]). Figure 3 illustrates the main 345
 features that characterize the gravitational instability in soft 346
 sediments: 347

[29] 1. Intrusions occur within essentially flat-lying layers 348
 (perpendicular to gravity) [Allen, 1985]. 349

[30] 2. Intrusions narrow from base to peak. 350

[31] 3. Layers are (originally) roughly planar, base of source 351
 layer remains smooth after intrusions form. In the particular 352
 case of Figure 3, the bottom of the unit is wavy because of the 353

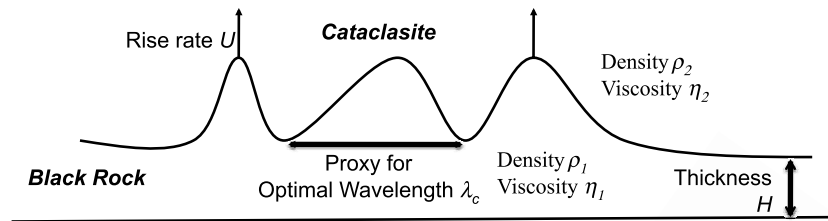


Figure 4. Geometry of the Rayleigh-Taylor problem. The densities ρ_1 and ρ_2 and viscosities η_1 and η_2 are of the lower and upper layers, respectively. The intrusions rise with a vertical velocity U .

354 sedimentary deformation of the layer below it, but this
355 waviness is unrelated to the flame structure formation.

356 [32] 4. The lower density layer is overlain by a higher-
357 density layer [Anketell *et al.*, 1970].

358 [33] 5. If intrusions are deflected, the direction of deflec-
359 tion is consistent [Anketell and Dzulyński, 1968; Potter and
360 Pettijohn, 1977].

361 [34] 6. Intrusion shape or size is not systematically
362 limited by rigid structure in denser layer; denser layer flows
363 to accommodate intrusions from less-dense layer.

364 [35] 7. Intrusions have a characteristic spacing [Allen,
365 1985].

366 2.4. Comparison of Fault Rock Intrusions 367 and Soft-Sediment Structures

368 [36] All seven of the criteria established above for soft
369 sediment instabilities are met by the black rocks in the fault
370 in Figure 2. The most striking difference is that the interval
371 between intrusions is much shorter relative to the layer
372 thickness in the fault rock case. We will return to this
373 observation in the flow analysis below.

374 [37] In other places on the fault zone, the black rocks
375 occur beneath consolidated metasandstone in the hanging
376 wall rather than cataclasite (Figure 1). These sandstones
377 were brittle at the conditions of deformation of the paleo-
378 decollement. The black rock injects into the sandstones but
379 the style and scale are distinct from the flame structures
380 case. These outcrops form a useful counterpoint that eluci-
381 dates the behavior of a viscous, low-density fluid layer
382 when the denser hanging wall is brittle rather than viscous.
383 The injections of ultrafine-grained material into the sand-
384 stone satisfy the first three criteria above: layered structure,
385 lower density material below, and (probably) near constant
386 thickness in the black rock layer. However, characteristics
387 of the sandstone-bounded intrusions violate the other four
388 criteria. The injection orientation and spacing are consistent
389 with activation of pre-existing joint patterns in the sand-
390 stone hanging wall. The outcrop where black rock underlies
391 a solid sandstone hanging wall does not at all resemble
392 sedimentary Rayleigh-Taylor instabilities, while the outcrop
393 where black rock underlies granular fault rocks closely
394 resembles it. Flame structure morphologies develop only
395 where both materials behave ductilely at the strain rate of
396 deformation.

398 3. Fluid Dynamics of the Rayleigh-Taylor 399 Instability

400 [38] The asymmetrical intrusions, like previously docu-
401 mented flame structures, imply that the driving force of the

402 flow is a density instability that can be used to analyze the
403 vertical motion of the black rock. The intrusion of a low-
404 density layer into an overlying high-density layer is a well-
405 studied phenomenon known as a Rayleigh-Taylor instability
406 [Turcotte and Schubert, 2002]. When the density of the
407 lower layer, ρ_1 , is less than that of the upper layer, ρ_2 , the
408 system is unstable and the lighter, black rock will intrude
409 into the cataclasite (Figure 4). The buoyancy forces are
410 balanced by viscous stress and the inertia of the fluid.

411 [39] The vertical velocity, U , of the intrusions varies with
412 the wavelength. Linear stability analysis shows that there is
413 generally an optimal wavelength, λ_c , that grows fastest and
414 thus dominates the resulting structure [Chandrasekhar,
415 1961; Conrad and Molnar, 1997; Turcotte and Schubert,
416 2002]. The linear stability analysis prediction of the optimal
417 wavelength is consistent with physical laboratory experi-
418 ments where the spacing between intrusions is interpreted as
419 the optimal wavelength [Berner *et al.*, 1972; Wilcock and
420 Whitehead, 1991]. If shearing is simultaneous, the intru-
421 sions will be inclined relative to the vertical; this horizontal
422 motion is independent of the buoyant growth that deter-
423 mines λ_c .

424 [40] We numerically solve for the growth rate $\gamma = U/H$ as
425 a function of wavelength for a viscous fluid of thickness H
426 overlain by an layer of denser viscous fluid for a variety of
427 geometries and rheologies as will be described below
428 (Figures 5–10). Success of the model will be measured
429 by the consistency of the computed optimal wavelength λ_c
430 with the observed spacing between black rock intrusions.
431 The spacing of the observed structures is used as a proxy for
432 optimal wavelength [Johnson and Fletcher, 1994]. As
433 reported in the Observations section, the spacing for the
434 Kodiak Island black rocks is 4.7 ± 1.5 cm and the layer
435 thickness is 3.5 ± 0.6 cm. Therefore the observed ratio λ_c/H
436 is 1.4 ± 0.5 (vertical gray line in Figure 5 with horizontal
437 error bars) (Division of the mean values was performed with
438 one additional significant digit than the final answer as is
439 required for intermediate computations. As a result, the
440 rounded value of the ratio is 1.4 rather than $4.7/3.5 =$
441 1.3.). If the peak of the growth rate curve as a function of
442 wavelength coincides with the observed value of λ_c/H
443 within the error range, the model will be interpreted as
444 successful. We will begin with a basic model and add
445 successive complications until we match the data.

446 3.1. Noninertial Flows

447 [41] We start with a configuration in which the top layer
448 is infinite and has the same viscosity as the lower layer. For
449 this first simple example, the viscosity of both layers is the
450 same, the fluids are Newtonian and inertia is assumed to be

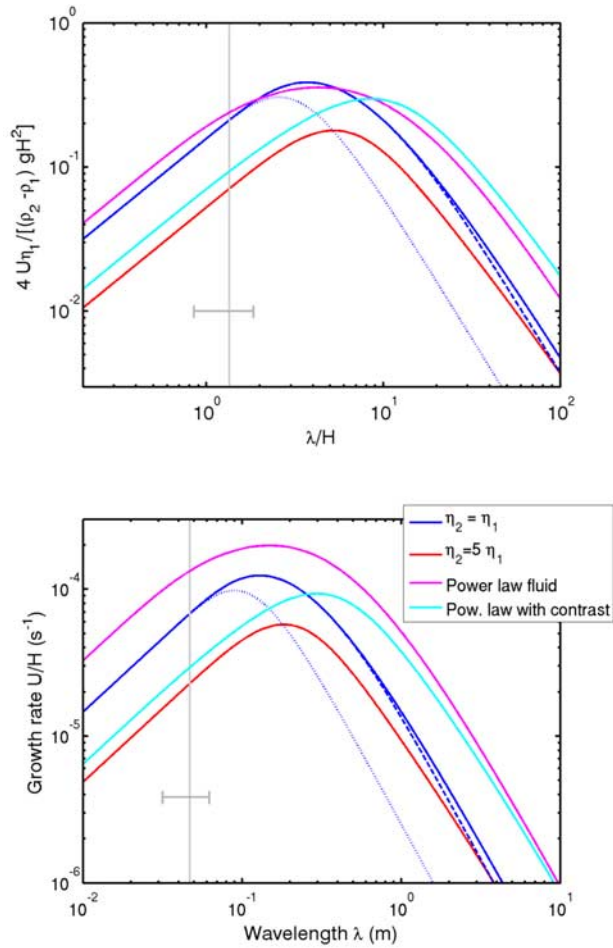


Figure 5. Growth rate of the instability as a function of wavelength for viscous (low Reynolds number) flows. (a) Dimensionless and (b) dimensional results shown for each case. Calculations are done with $H = 0.035$ m, $\rho_1 = 2685$ kg/m 3 , $\rho_2 = 1.014\rho_1$, and $\eta_1 = 10^4$ Pa s. For the power law fluid with no contrast, $\eta_0 = 10^4$ Pa n s and $n = 5$ and for the contrast case, $\eta_0 = 10^4$ Pa n s and $n = 1.5$ in the black rock and $\eta_0 = 5 \times 10^4$ Pa n s and $n = 5$ in the cataclasite. As discussed in the text, the blue solid line in Figure 5a is nondimensionalized to be independent of these material properties as long as inertia is negligible. The dotted and dashed lines are for two layers of finite thickness and equal viscosity. The top layer is the same thickness as the bottom for the dotted line (0.035 m) and is 0.3 m (the observed thickness of the textural domain in the cataclasite) for the dashed line. The gravitational acceleration g is 9.8 m/s 2 . None of the modeled curves shown successfully match the data.

451 negligible. The boundary conditions for this and all
 452 subsequent calculations are no-slip at the top and bottom
 453 of the system (Appendix A). As the gravitational instability
 454 is inherently asymmetric with no flow downwards, a zero
 455 velocity boundary condition on the vertical velocity is
 456 appropriate at the base of the low-density layer. Figure 5
 457 shows the results in both dimensionless form and with units
 458 appropriate for the Kodiak Island black rock. For the single-
 459 viscosity case, a single dimensionless curve completely

describes the solution (dark blue solid curve) [Turcotte 460
 and Schubert, 2002]. The most unstable wavelength $\lambda_c = 461$
 3.7 H , which is inconsistent with the observed range. Note 462
 that λ_c/H is independent of viscosity and density. Making 463
 the top layer finite (dotted and dashed lines) does not 464
 significantly change the value of λ_c/H . 465

[42] A more realistic model incorporates the viscosity 466
 contrast in rheologies between the black rock and the 467
 cataclasite. As discussed above, the black rock is more 468
 stretched and cusped than the cataclasite and therefore we 469
 infer that the black rock is the less viscous of the two layers. 470
 Incorporating this complication increases the value λ_c/H as 471
 shown by the red curve in Figure 5. Therefore the contrast 472
 in viscosity results in modeled optimal wavelengths even 473
 further from observed spacing than in the single-viscosity 474
 case. 475

[43] In a further effort to match the observations, we add 476
 the complication of a non-Newtonian rheology. We model 477
 both the black rock and the cataclasite as power law fluids 478
 where the strain rate is proportional to shear stress to the 479

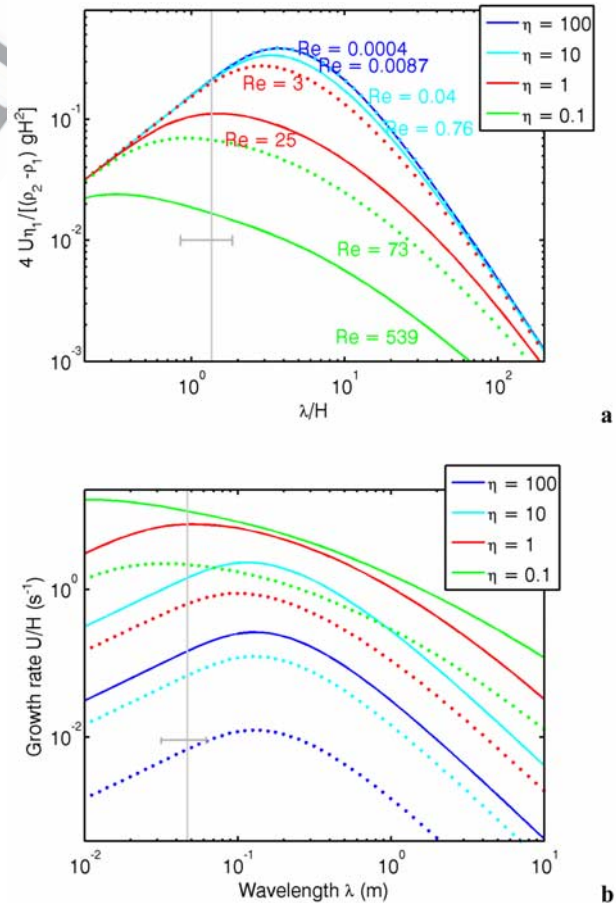
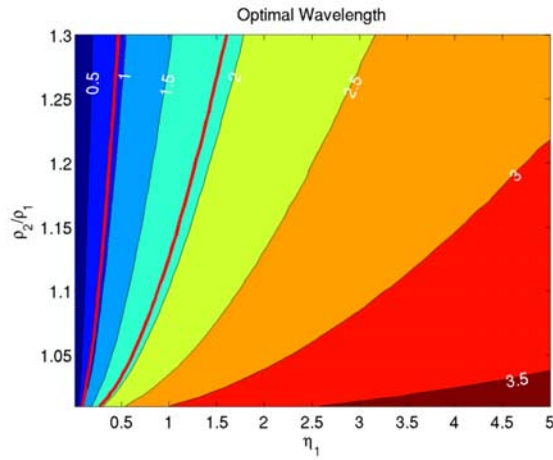
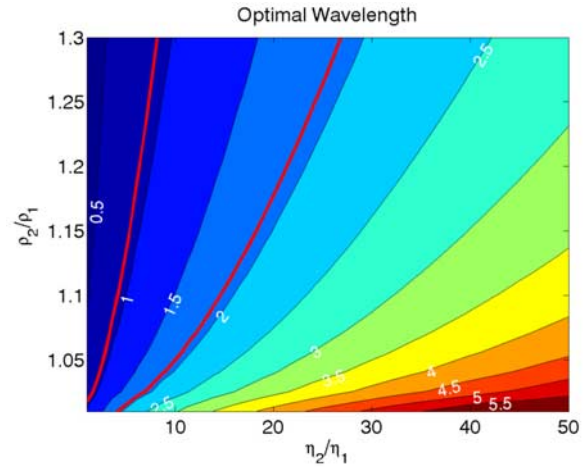


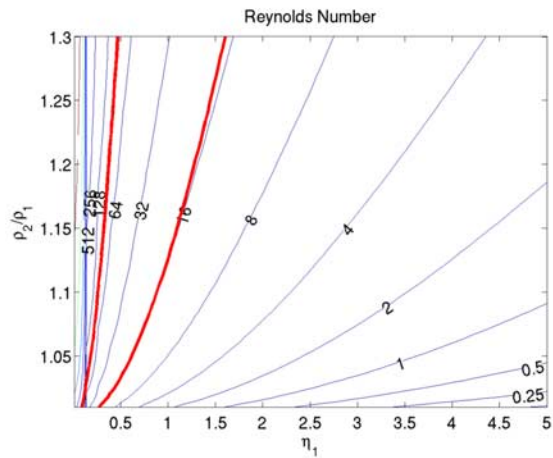
Figure 6. Growth rate of the instability as a function of wavelength for a variety of Reynolds numbers. (a) Dimensionless and (b) dimensional results for identical viscosity in both layers. Plus symbols are a density contrast of 1.4% and solid lines are 30% for each case. As in Figure 5, the thickness of the bottom layer is 0.035 m, the top layer is infinite, and $\rho_1 = 2685$ kg/m 3 . The Reynolds numbers Re are given for the most unstable wavelength of each curve.



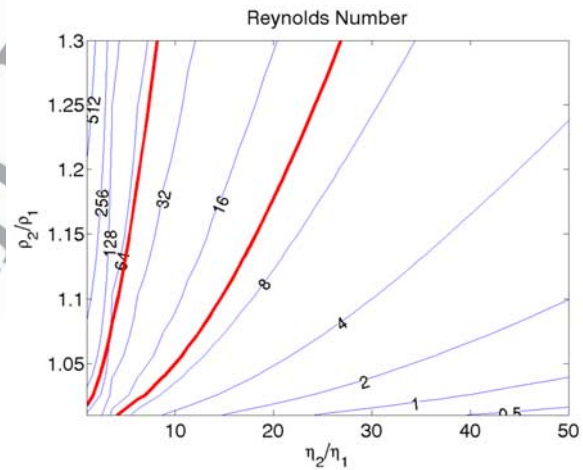
a



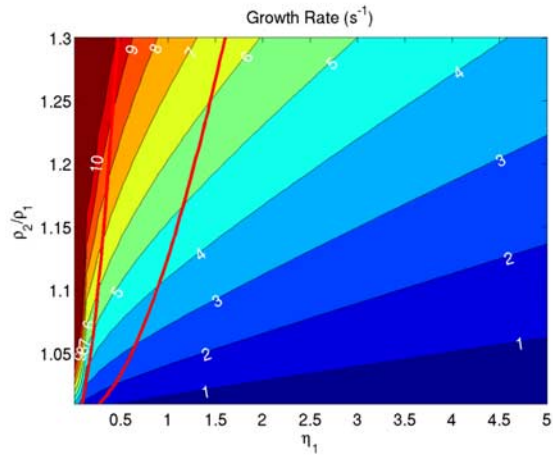
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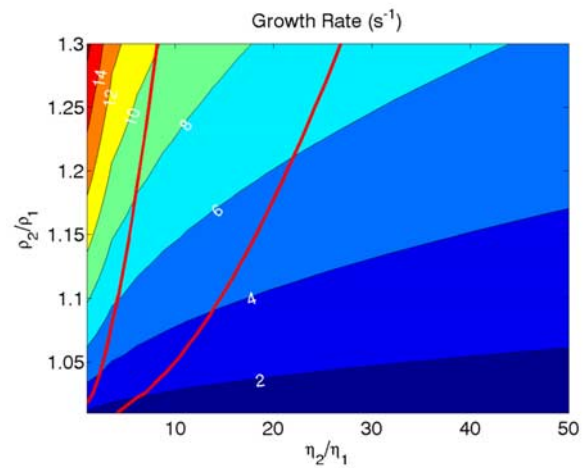
b



b



c



c

Figure 7. Contours of the model results as a function of density ratio and viscosity for single-viscosity models with nonnegligible inertia. (a) Optimal wavelength corresponding to the peak growth rate. Wavelength is normalized by the layer thickness (0.035 m) and is therefore dimensionless. (b) Reynolds numbers. (c) Growth rates. Thick red lines outline the region with optimal wavelength consistent with the observed range of intrusion spacing (wavelength to thickness ratio = 0.9–1.9). Reynolds number contours in Figure 7b are by factors of 2, with the 4 highest contours on the plot unlabeled to prevent overlapping numbers.

Figure 8. Contours of the model results as a function of viscosity ratio and density ratio for fixed values of viscosity in the black rock layer of 0.1 Pa s. (a) Optimal wavelength corresponding to the peak growth rate. Wavelength is normalized by the layer thickness (0.035 m) and is therefore dimensionless. (b) Reynolds numbers in the cataclasis. (c) Growth rates. Thick red lines outline the region with optimal wavelength consistent with the observed range of intrusion spacing (0.9–1.9).

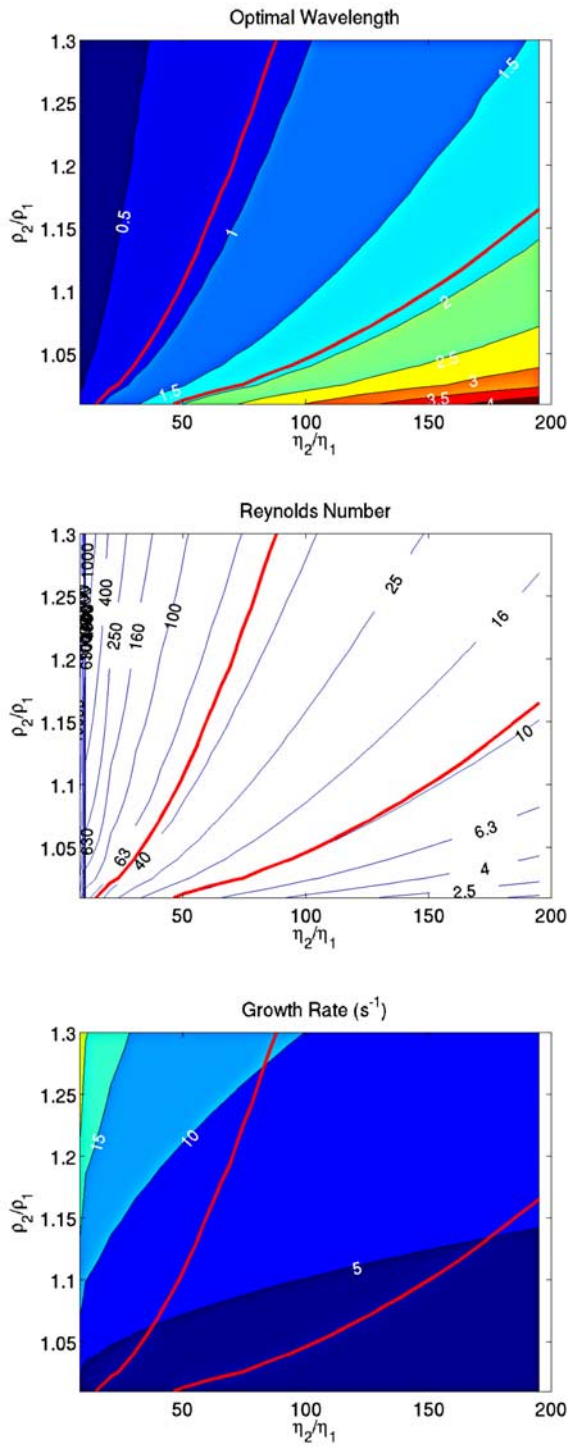


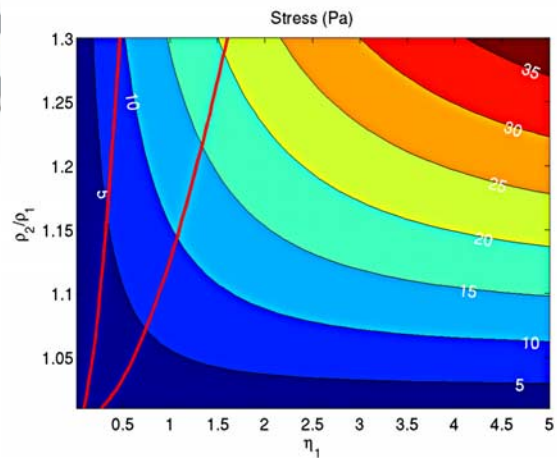
Figure 9. Contours of model results for a smaller value of the black rock viscosity of 0.01 Pa s. (a) Optimal wavelength corresponding to the peak growth rate. Wavelength is normalized by the layer thickness (0.035 m) and is therefore dimensionless. (b) Reynolds numbers in the cataclasite. (c) Growth rates. Thick red lines outline the region with optimal wavelength consistent with the observed range of intrusion spacing (0.9–1.9).

power of n ($n = 1$ for a Newtonian fluid) using a modification of a standard analysis for folding and boudinage [Smith, 1977] (Appendix A). In this rheology, the effective viscosity at a given strain rate γ is $\eta_0^{1/n} \gamma^{(1/n)-1}$ where η_0 is a constant. Magma can have $n = 1.5$ and solid state rocks can have $n = 2-5$. Figure 5 shows the most extreme case with $n = 5$ in both layers as the pink curve [Sonder et al., 2006; Twiss and Moores, 1992]. The wavelength of the maximum growth is nearly unaffected by the rheology ($\lambda_c/H = 4.3$). Nondimensionalizing as before with η_1 equal to the effective viscosity at the peak growth rate results in a broader peak with the nondimensional maximum growth consistent with the Newtonian model (Figure 5a). We also investigate a difference in power law exponents in the top and bottom layers. As in the Newtonian case, if the effective viscosity of the upper layer is higher (as required by the data), then the value of λ_c/H increases. Although only a few model cases are shown here, they illustrate that the trend of the non-Newtonian effect runs counter to that required by the data.

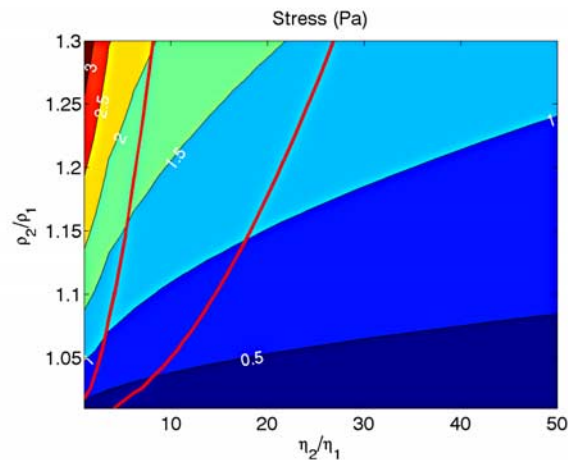
a

b

c



a



b

Figure 10. Viscous stress in the lower layer (black rock) assuming that the horizontal strain rate is the same as the vertical (see text). (a) Single-viscosity model corresponding to Figure 7. (b) Dual viscosity model with lower layer viscosity of 0.1 Pa s corresponding to Figure 8.

[44] In summary, the model results thus far show that the real system has a spacing between intrusions that is much shorter than can be explained easily by a Rayleigh-Taylor instability model without inertia. This result holds true even if we consider a finite thickness of the upper layer, a viscosity contrast between the layers or a non-Newtonian rheology. Therefore we conclude that the noninertial model is a poor fit to the observed structures.

3.2. Inertial Flows

[45] Inertial flows have a broader spectrum of unstable wavelengths and the most unstable value is smaller than in the purely viscous case. Using the theory of Chandrasekhar [1961] and Mikaelian [1996], we repeat the calculation of growth rate as a function of wavelength for parameter ranges where the inertial effects are significant (Figure 6). The Reynolds number, Re , measures the relative strength of the inertial and viscous effects. For the present problem, $Re = UH\rho_2/\eta_2$ where the subscript of 2 indicates the values in the upper layer and Re values greater than 1 indicate that inertia is important. Since the values of H and ρ are constrained by the observations and U is computed by the flow calculations, the most straightforward way to adjust the Reynolds number of the modeled flow is to manipulate the viscosity.

[46] As in the noninertial case, we begin the modeling exercise with the unrealistic, but simple assumption that both layers have the same Newtonian viscosity (Figures 6a and 6b). In the examples shown, flows with moderate Reynolds numbers like 25 and 73 have peak growth rates at wavelengths consistent with the observations for the range of plausible densities (Figures 6a and 6b). This result is reinforced by an exploration of optimal wavelength as a function of density contrast and viscosity in Figure 7a. The contours of optimal wavelength track the contours of Reynolds number in the cataclasite (Figure 7b). The stiffer, thicker layer limits the spacing between intrusions. The flows with moderate Reynolds numbers of 16–86 have optimal wavelengths within the observational range marked by the thick red curves. This range corresponds to a restricted range of growth rates of $1-10\text{ s}^{-1}$ (Figure 7c).

[47] As in the noninertial case, incorporating the observed viscosity contrast increases the optimal wavelength for a given density contrast and black rock viscosity. The trade-off between viscosity contrast and density contrast is mapped out in Figure 8 for a fixed lower layer (black rock) viscosity of 0.1 Pa s as an example. The Reynolds number in the upper layer (cataclasite) is still a good predictor of the optimal wavelength (Figures 8a and 8b). Flows that match the data have Reynolds numbers of 10–51.

[48] The growth rate of the intrusions is also constrained by the flow model and the observed data. For the range of acceptable density contrasts with viscosity ratios corresponding to the upper layer Reynolds number of 10–51, the growth rates are $1-10\text{ s}^{-1}$ (Figure 8c). This result is only weakly sensitive to the viscosity in the lower layer as illustrated by Figure 9. Here the lower layer viscosity is fixed an order of magnitude smaller than in the previous example, and the Reynolds number range and growth rate range matching the data is nearly the same ($Re = 10-49$, growth rate = $1-10\text{ s}^{-1}$).

[49] The strain rate multiplied by the thickness of the black rock layer H is the vertical rise velocity at the onset of the instability. For $H = 0.035\text{ m}$, the initial rise velocity corresponding to Figures 7–9 is therefore $0.04-0.4\text{ m/s}$, depending on the viscosity conditions. The horizontal shear rate and vertical growth rate are comparable, so the structures were generated at a slip rate of 10s of cm/s, which is typical of an earthquake or immediately after. Thus the black rock was mobilized during an earthquake. The fluidization could have occurred by a variety of processes including melting, elevated pore pressure or intergranular collision [Bagnold, 1956; Otsuki et al., 2003]. The exposure preserves the structures solidified after the generation of the fluid and thus represents the last stages of the earthquake slip. Once fluidized, it moved rapidly and buoyantly intruded the overlying cataclasite at a moderate Reynolds number.

[50] The viscous shear stress in a fluid layer is twice the product of the strain rate and viscosity (Figure 10). Here we use the inference that the shear strain rate in the black rock is similar to the growth rate of the rising instabilities. The growth rate is well-constrained as $1-10\text{ s}^{-1}$ by the intrusion spacing data, but the lower layer viscosity is only weakly constrained. The most certain inference is that the lower layer (black rock) has a lower effective viscosity than the upper layer (cataclasite). The maximum value of the upper layer viscosity is provided by the single-viscosity case. The highest viscosity that results in sufficient inertia (Reynolds number) to match the data is 1.5 Pa s (Figure 7a) and the corresponding stress is 20 Pa (Figure 10a). Therefore the maximum bound of the viscous stress in the lower layer (black rock) is 20 Pa .

4. Origin of the Black Rock

[51] Having constrained the viscosity of the black rock, we can now use it to evaluate the candidate origins of the black rock. Pseudotachylytes (frictionally-induced melts) are one of few established features used to infer rapid slip from geologic data [Biegel and Sammis, 2004; Cowan, 1999; Di Toro et al., 2005; Magloughlin, 1992; Sibson and Toy, 2006]. However, pseudotachylytes are apparently rare and their identification is difficult [Otsuki et al., 2003; Sibson and Toy, 2006; Ujiie et al., 2007a]. We can calculate the required temperature for a melt of the observed composition, pressure and fluid conditions to achieve the geometrically constrained viscosity. Should the inferred temperature be plausible, then pseudotachylytes are a permissible mechanism.

[52] The high pressure and water content of the accretionary prism permits fully saturated melts of unusually high water contents. The black rock composition is equivalent to a high silica andesite (Table B1). At 380 MPa (13 km) and 1400°C , a melt of the composition of the black rock is fully saturated with 6.6 wt\% water and has a viscosity of 1 Pa s (Appendix B). A pseudotachylyte at these conditions is consistent with the spacing constraint of the intrusions. Such a high temperature is also consistent with the minimum bound of 1100°C imposed by the rarity of feldspar survivor grains in the black rock [Rowe et al., 2005]. The inferred temperature and water content is consistent with that inferred for fault slurries with local

t.2.1 **Table 2.** Parameters for Energy Balance Calculations (Equation (1))^a

t.2.2	Parameter	Value
t.2.3	Specific heat capacity c_p	$4 \times 10^3 \text{ J/}^\circ\text{C kg}$
t.2.4	Thickness of black rock h	0.029–0.041 m
t.2.5	Density of black rock ρ	2700 kg/m ³
t.2.6	Latent heat L	0.3 MPa
t.2.7	Coefficient of friction	0.2–0.6
t.2.8	Lithostatic Pressure P_L	320–380 MPa
t.2.9	Slip D	5–10 m

^aSpecific heat and latent heat are from *Turcotte and Schubert* [2002]. The thickness range of the black rock encompasses 1 standard deviation of measurements. The range of coefficient of frictions spans current high-speed laboratory values through typical Byerlee Law values [*Byerlee*, 1970; *Yuan and Prakash*, 2008]. The density of the black rock is rounded from Table 1. Lithostatic pressure is calculated for 12–14 km. Slip is a typical range during a single large earthquake (M_w 7.5–8.5).

621 melting observed in the Nojima fault and similar to the
622 Shimanto accretionary complex [*Otsuki et al.*, 2003; *Ujiie et*
623 *al.*, 2007b].

624 [53] Lower viscosities of the melt are also permissible in the
625 flow model, but require extraordinarily high temperatures. A
626 viscosity of 0.1 Pa s corresponds to a temperature of 1900°C
627 fully saturated at the same pressure conditions as above.

628 [54] High temperatures can be generated by the frictional
629 heat of the fault during a large earthquake in part because of
630 the great depth of the fault implies an unusually high
631 frictional heat. The pre-slip temperature of the fault based
632 on fluid inclusions is 270°C, thus a temperature increase of
633 at least 1130°C is necessary to satisfy the petrologic con-
634 straints [*Vrolijk et al.*, 1988]. A naïve calculation of the
635 temperature increase in a melt during the earthquake balan-
636 ces the excess temperature and latent heat with the frictional
637 heat generated.

$$\Delta T c_p h \rho + L h \rho = \mu P_L D \quad (1)$$

639 where ΔT is the temperature increase over the preseismic
640 temperature, c_p is the specific heat capacity, h is the
641 thickness of the melt zone, ρ is the density of the melt, L is
642 the latent heat, μ is the coefficient of friction, P_L is the
643 lithostatic pressure and D is the slip. Using the parameters in
644 Table 2, equation (1) results in a range of temperature
645 increases of 600–7000°C. As pointed out by *Fialko and*
646 *Khazan* [2005], this simplistic calculation overestimates the
647 heat produced as the shear resistance drops dramatically on
648 the wetted surface once melting begins. The calculation
649 only demonstrates that in a system with some areas in solid
650 contact ample energy is available for the elevated
651 temperatures implied by the rheology.

652 [55] Another possible origin of the fault rock is as a
653 fluidized granular flow where either an aqueous fluid is
654 sufficiently pressurized to support the matrix or the inertial
655 collisions of the grains maintains a non-Newtonian viscosity
656 [*Rowe et al.*, 2005; *Ujiie et al.*, 2007a]. Unfortunately,
657 comparable constraints on the physical conditions of a
658 fluidized granular flow are not possible as the rheology
659 has never been investigated at the appropriate pressure,
660 temperature and speeds. The little experimental data that
661 exists at atmospheric pressure on laboratory debris flows
662 reports that mobilized slurries at strain rates $>5 \text{ s}^{-1}$ and
663 sediment volume concentrations of 40–70% have effective

viscosities of $\sim 1\text{--}10 \text{ Pa s}$ [*Major and Pierson*, 1992]. The
lower bound of this viscosity range is consistent with the
rheological constraints here.

[56] We therefore conclude that either the fluidized slurry
or the extremely high-temperature ($\geq 1400^\circ\text{C}$) melt are
consistent with the rheological constraints on the black
rock. The geometry may not help resolve the question of
the origin of the black rocks, but the consistency with
plausible regimes in both cases helps bolster the Rayleigh-
Taylor interpretation of the flow.

5. Summary and Conclusions

[57] The extremely short spacing of the intrusions ob-
served on the exhumed Kodiak Island megathrust indicate
that the black fault core rocks represent a very low viscosity
($\leq 1 \text{ Pa s}$) fluid emplaced during an earthquake. This
conclusion is based on the geometry of the intrusive
structures and supported by measurements of the densities
of the units. No prior knowledge of the origin of the fault
rock is necessary.

[58] Although the buoyant intrusive features are only
formed where the overlying cataclastite is fluid enough to
accommodate ductile intrusions, the black rock persists over
2.5 km of strike-parallel exposure. Elsewhere on the fault,
direct contact between the wall rocks may have resulted in
high shear stresses, but were the black rock is present the
fault was lubricated with a fluid that supported little shear
($< 20 \text{ Pa}$).

[59] The rock record has provided an example of extreme
fault weakening that easily satisfies geophysical constraints
suggesting low friction as well as petrological constraints on
the material properties of a silicate melt or granular flow.
The picture that begins to emerge is a fault zone controlled
by multiphase processes including local, extraordinarily
weak zones of low-viscosity fault fluids flowing rapidly
during an earthquake.

Appendix A: Linear Stability Analysis

[60] The main text solves four closely related linear
stability problems: the buoyant intrusion of a Newtonian
fluid into another Newtonian fluid for both finite and
infinite overlying layers, the buoyant intrusion of a power
law fluid into another power law fluid and the buoyant
intrusion of a Newtonian fluid into an infinite Newtonian
fluid with inertia. All of the Newtonian fluid configurations
have either been solved in the literature or require only
minor modifications of existing solutions. The power law
fluid case requires a more significant modification.

[61] The general solution method is outlined below. Here
we primarily follow the notation of *Smith* [1977] who
studied the closely related problem of viscous folding. For
a Newtonian fluid with negligible inertia, combining the
momentum and continuity equations results in the bihar-
monic equation

$$\nabla^4 \psi = 0 \quad (\text{A1})$$

where ψ is the stream function. The velocity field of the
fluid is $u = \frac{\partial \psi}{\partial y}$ and $v = \frac{\partial \psi}{\partial x}$ where v is the flow velocity in
the x direction and u is the flow velocity in the y direction.

720 The shear measurements indicate that vertical growth rate u
 721 is comparable to horizontal shear rate v , establishing a basis
 722 for control on v . The linear stability of the system is
 723 investigated by assuming a separable solution to ψ of the
 724 form $\psi(x,y,t) = \varphi(y) \exp[iax] \exp[\gamma t]$ where $\varphi(y)$ is an
 725 appropriate function of y , γ is the growth rate, the
 726 wavenumber $a = 2\pi/\lambda$ and λ is the wavelength. The growth
 727 rate is in units of strain rate, i.e., 1/time. Surface tension is
 728 neglected.

729 [62] Substituting ψ into equation (A1) results in

$$\varphi'''' - 2a^2\varphi'' + a^4\varphi = 0 \quad (\text{A2})$$

$$M = \begin{bmatrix} 1 & 0 & 1 & 0 & 0 & 0 \\ -a & 1 & a & 1 & 0 & 0 \\ -e^{-ah} & -e^{-ah}h & -e^{ah} & -e^{ah}h & e^{-ah} & e^{-ah}h \\ ae^{-ah} & e^{-ah}(ah-1) & -ae^{ah} & -e^{ah}(1+ah) & -ae^{-ah} & e^{-ah}(1-ah) \\ 2a^2e^{-ah}m & 2ae^{-ah}(ah-1)m & 2a^2e^{ah}m & 2ae^{ah}(1+ah)m & -2a^2e^{-ah} & -2ae^{-ah}(ah-1) \\ 2a^3e^{-ah}m & 2a^3e^{-ah}hm & -2a^3e^{ah}m & -2a^3e^{ah}hm & \frac{a^2e^{-ah}(\Delta\rho g - 2a\gamma\eta_1)}{\gamma\eta_1} & \frac{a^2e^{-ah}h(\Delta\rho g - 2a\gamma\eta_1)}{\gamma\eta_1} \end{bmatrix} \quad (\text{A11})$$

731 where primes are derivatives with respect to y . The
 732 boundary conditions can also be posed in terms of φ . The
 733 coordinate system is chosen such that the bottom of layer 1
 734 is $y = 0$. The thickness of layer 1 is h and if the top layer is
 735 finite, the thickness of the two layers together is h_2 . There is
 736 no slip and a continuity of traction between the layers, so
 737 the boundary conditions at $y = h$ are

$$\varphi_1 = \varphi_2 \quad (\text{A3})$$

$$\varphi'_1 = \varphi'_2 \quad (\text{A4})$$

$$(\varphi''_1 + a^2\varphi_1) = m(\varphi''_2 + a^2\varphi_2) \quad (\text{A5})$$

$$(\varphi'''_1 - 3a^2\varphi_1) - m(\varphi'''_2 - 3a^2\varphi_2) = -\Delta\rho g a^2\varphi_1/\gamma\eta_1 \quad (\text{A6})$$

745 where the subscripts 1 and 2 indicate the bottom and top
 746 layer, respectively, $\Delta\rho$ is the density difference between the
 747 top and bottom layer ($\rho_2 - \rho_1$), η_1 is the viscosity of the
 748 bottom layer and m is the ratio of the viscosities ($m = \eta_2/\eta_1$).
 749 Note that the subscript convention is reversed from *Smith*
 750 [1977]. The last boundary condition equation (A6) comes
 751 from the stress equilibrium at the interface and incorporates
 752 buoyancy [*Conrad and Molnar*, 1997]. This term is the
 753 most important difference between the folding problem of
 754 *Smith* [1977] and the gravitational instability studied here.

755 [63] An appropriate form of $\varphi(y)$ that respects the bound-
 756 ary conditions must be chosen. For the Newtonian cases,
 757 $\varphi(y) = A \exp[ay] + B y \exp[ay] + C \exp[-ay] + D y$
 758 $\exp[-ay]$. If the top layer is infinite, $A = B = 0$ in that layer
 759 (layer 2). Otherwise, at the top of the layer $y = h_2$, no slip is
 760 achieved by

$$\varphi_2 = 0 \quad (\text{A7})$$

$$\varphi'_2 = 0 \quad (\text{A8})$$

[64] The no slip condition at the bottom of the lower 764
 boundary is achieved at $y = 0$ with the equations 765

$$\varphi_1 = 0 \quad (\text{A9})$$

$$\varphi'_1 = 0 \quad (\text{A10})$$

[65] The solution for the growth rate γ as a function of 770
 wavenumber a is found by posing the boundary conditions 771
 as a matrix system $MG = 0$ where G is the vector of constant 772
 coefficients (A, B, D and E for each layer). For instance, for 773
 the case of an infinite top layer, the matrix 774

[66] Solving the equation $\text{Det}(M) = 0$ provides a solution 777
 for the growth rate γ as a function of wavenumber a . We 778
 solve this equation numerically for every case although 779
 analytical solutions are possible for the simplest configu- 780
 rations studied here. 781

[67] For power law fluids the rheology is $\sigma'' \propto \dot{\epsilon}$ where σ 782
 and $\dot{\epsilon}$ are the stress and strain rate tensors and n is a material 783
 constant. *Smith* [1977] performs a perturbation on the 784
 rheology as well as the deformation field for a basic flow 785
 of horizontal compression or extension. He shows that the 786
 linear stability equations are similar to the Newtonian fluid 787
 case. We extend the analysis for a basic flow of simple 788
 shear. In this case, the equations are identical to the New- 789
 tonian fluid case except equation (A6) becomes 790

$$\begin{aligned} (\varphi'''_1 - (2W_1 + 1)a^2\varphi'_1) - m(\varphi'''_2 - (2W_2 + 1)a^2\varphi'_2) \\ = -n\Delta\rho g a^2\varphi_1/\gamma\eta_1 \end{aligned} \quad (\text{A12})$$

where $W = 2n - 1$ and the subscripts of 1 and 2 denote 792
 the bottom and top layers, respectively. In this case, the 793
 function $\varphi(y) = \sum_{i=1,4} A_i \exp[l_i y]$ where l_i are the four 794
 values of $\pm a\sqrt{W \pm \sqrt{W^2 - 1}}$ for each layer [*Smith*, 1977]. 795

[68] For the high Reynolds number case, the inertial term 796
 makes the right-hand side of equation (A1) nonzero and a 797
 stream function is no longer an appropriate tool for solving 798
 the problem. *Chandrasekhar* [1961] uses a similar method 799
 based on a perturbation expansion of the flow velocity 800
 rather than the stream function. He explores the case with 801
 negligible advection, but significant inertia from the local 802
 acceleration of the fluid. The eigenfunctions in this case 803
 include an inertial term [*Chandrasekhar*, 1961, section 94]. 804
 This method is used here with the modifications for a finite 805
 layer on the bottom introduced by *Mikaelian* [1996]. These 806
 theories only address the Newtonian fluid case. 807

Appendix B: Melt Viscosity and Density Calculation 808 809

[69] We calculated the viscosity of a silicate melt with the 810
 bulk composition measured from the black rock samples 811

t3.1 **Table B1.** Composition Kodiak Island Black Rock and Foliated Cataclasites^a

t3.2	Oxides	Black Rock Weight %		Cataclasite Weight %	
		Mean	Standard Deviation	Mean	Standard Deviation
t3.3					
t3.4	SiO ₂	58.53	1.99	59.07	0.96
t3.5	TiO ₂	0.94	0.04	0.83	0.03
t3.6	Al ₂ O ₃	17.80	0.63	16.70	0.60
t3.7	FeO	6.71	0.20	6.57	0.54
t3.8	Fe ₂ O ₃	0.20	0.23	0.56	0.55
t3.9	MnO	0.20	0.23	0.15	0.06
t3.10	MgO	2.84	0.81	2.96	0.55
t3.11	CaO	1.42	0.73	1.77	0.79
t3.12	Na ₂ O	4.01	0.98	2.19	0.78
t3.13	K ₂ O	1.60	1.01	2.45	0.88
t3.14	P ₂ O ₅	0.25	0.02	0.24	0.04
t3.15	Lost on ignition	4.95	0.45	4.78	0.37
t3.16	Total	99.26		99.39	

^aWhole rock geochemical analyses of major and trace elements were determined by wavelength dispersive X-ray fluorescence (WD-XRF) analysis with a Philips PW2400 equipped with Rhodium tube (Department of Mineralogy and Petrology, University of Padova). For analysis, powder samples were mixed and diluted at 1:10 with Li₂B₄O₇ and LiBO₂ flux and melted into glass beads. Loss on ignition (LOI) was determined from weight lost after ignition at 860°C for 20 min and at 980°C for 2 h. FeO was determined with permanganometry using a Rhodium tube. International rock standards were used for calibration. Four samples were analyzed for the black rock and eight for the cataclasite.

812 (Table B1) using the program Conflow [Mastin and
813 Ghiorso, 2000]. We renormalize the composition to
814 100% without the loss on ignition (LOI) and find that the
815 composition is equivalent to a high silica andesite. Conflow
816 implements the MELTS algorithm to minimize the energy
817 of the silicate melt-water mixture using laboratory values
818 for the thermodynamic properties [Ghiorso and Sack, 1995].
819 The energy minimization yields the water solubility at a
820 given pressure, temperature and composition. The result is
821 then used to calculate the viscosity for the appropriate
822 composition in accordance with Shaw [1972]. MELTS also
823 calculates the melt density at the prescribed temperature,
824 pressure and water content by again combining empirical
825 laboratory data with thermodynamic constraints.
826 [70] The volume percentage of survivor grains from the
827 pre-melted structure was measured in thin sections. The
828 resulting percentage of clasts during melt mobilization is
829 <<10%, therefore, the melt viscosity is a good indicator of
830 the mixture viscosity. At the emplacement conditions
831 (380 MPa, water-saturated), the temperature must be
832 1450°C to achieve a viscosity of 1 Pa s with 10% solid
833 fragments.

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841 References

842 Abercrombie, R. E., et al. (Eds.) (2006), Earthquakes: Radiated energy and
843 the physics of faulting, *Geophys. Monogr. Ser.*, vol. 170.
844 Allen, J. R. L. (1982), *Sedimentary Structures: Their Character and Physical Basis*, vol. 2, 663 pp., Elsevier, New York.
845 Allen, J. R. L. (1985), *Principles of Physical Sedimentology*, 272 pp.,
846 George Allen and Unwin Ltd.

Andrews, D. J. (2002), A fault constitutive relation accounting for thermal
pressurization of pore fluid, *J. Geophys. Res.*, 107(B12), 2363,
doi:10.1029/2002JB001942. 848
849
850
Anketell, J. M., and S. Dzylinski (1968), Transverse deformational patterns
in unstable sediments, *Ann. Soc. Geol. Pol.*, 38, 411–416. 851
852
Anketell, J. M., et al. (1970), On the deformational structures in systems
with reversed density gradients, *Ann. Soc. Geol. Pol.*, 40, 3–30. 853
854
Bagnold, R. A. (1956), The flow of cohesionless grains in fluids, *Philos.*
Trans. R. Soc. London, Ser. A, 249(964), 235–297. 855
856
Berner, H., et al. (1972), Diapirism in theory and experiment, *Tectonophy-*
sics, 15, 197–218. 857
858
Bhattacharya, H. N., and S. Bandyopadhyay (1998), Seismites in a Proter-
ozoic tidal succession, Singhbhum, Bihar, India, Sediment. Geol., 119,
239–252. 859
860
Biegel, R. L., and C. G. Sammis (2004), Relating fault mechanics to fault
zone structure, *Adv. Geophys.*, 47, 65–111. 862
863
Brodsky, E. E., and H. Kanamori (2001), Elastohydrodynamic lubrication
of faults, *J. Geophys. Res.*, 106(B8), 16,357–16,374. 864
865
Brodzikowski, K., and A. Haluszczak (1987), Flame structures and
associated deformations in Quaternary glaciolacustrine and glaciodeltaic
deposits: Examples from central Poland, *Geol. Soc. Lond. Spec. Publ.*,
29(1), 279–286. 866
867
Byerlee, J. D. (1970), Static and kinetic friction of granite at high normal
stress, *Inst. J. Rock Mech. Min. Sci.*, 7, 3821–3827. 870
871
Byrne, T. (1984), Early deformation in melange terranes of the Ghost Rocks
Formation, Kodiak Islands, Alaska (Special Paper), *Geol. Soc. Am.*, 198,
21–51. 872
873
874
Chandrasekhar, S. (1961), *Hydrodynamic and Hydromagnetic Stability*,
Dover, Mineola, New York. 875
876
Clifton, H. E. (1984), Sedimentation units in stratified resedimentation
conglomerate, Paleocene submarine canyon fill, Point Lobos, California,
paper presented at Sedimentology of Gravels and Conglomerates, Mem-
oir-Canadian Society of Petroleum Geologists, Hamilton, ON, Canada. 877
878
Collinson, J. (1994), Sedimentary deformational structures, in *The Geologi-*
cal Deformation of Sediments, edited by A. Maltman, pp. 95–125,
Chapman and Hall, London, U.K. 882
883
Conrad, C. P., and P. Molnar (1997), The growth of Rayleigh-Taylor-type
instabilities in the lithosphere for various rheological and density struc-
tures, Geophys. J. Int., 129, 95–112. 884
885
886
Cowan, D. S. (1999), Do faults preserve a record of seismic slip? A field
geologist's opinion, *J. Struct. Geol.*, 21(8–9), 995–1001. 887
888
Dasgupta, P. (1998), Recumbent flame structures in the Lower Gondwana
rocks of the Jharia Basin, India—A plausible origin, *Sediment. Geol.*,
119, 253–261. 889
890
891
Davis, G. H., and S. J. Reynolds (1996), *Structural Geology of Rocks and*
Regions, 2nd ed., John Wiley, Hoboken, N. J. 892
893
Di Toro, G., et al. (2005), Can pseudotachylytes be used to infer earthquake
source parameters? An example of limitations in the study of exhumed
faults, *Tectonophysics*, 402(1–4), 3–20. 894
895
896
Dieterich, J. H., and E. T. Onat (1969), Slow finite deformations of viscous
solids, *J. Geophys. Res.*, 74(8), 2081–2088. 897
898
Fialko, Y., and Y. Khazan (2005), Fusion by earthquake fault friction: Stick or
slip?, *J. Geophys. Res.*, 110, B12407, doi:10.1029/2005JB003869. 899
900
Ghiorso, M. S., and R. O. Sack (1995), Chemical mass transfer in magmatic
processes. IV: A revised and internally consistent thermodynamic model
for the interpolation and extrapolation of liquid-solid equilibria in mag-
matic systems at elevated temperatures and pressures, Contrib. Mineral.
Petrol., 119. 901
902
903
904
905
Horváth, Z., et al. (2005), Soft-sediment deformation structures in the
Late Miocene-Pleistocene sediments on the pediment of the Mátra Hills
(Visonta, Atkár, Verseg): Cryoturbation, load structures or seismites?,
Tectonophysics, 410, 81–95. 906
907
908
909
Johnson, A. M., and R. C. Fletcher (1994), *Folding of Viscous Layers:*
Mechanical Analysis and Interpretation of Structures in Deformed Rock,
Columbia Univ. Press, New York. 910
911
912
Kelling, G., and E. K. Walton (1957), Load-cast structures; their relation-
ship to upper-surface structures and their mode of formation, *Geol. Mag.*,
94(6), 481–490. 913
914
915
Lachenbruch, A. H., and J. H. Sass (1980), Heat flow and energetics of the
San Andreas fault zone, *J. Geophys. Res.*, 85(B11), 6185–6222. 916
917
Lachenbruch, A. H., and J. H. Sass (1992), Heat flow from Cajon Pass,
fault strength, and tectonic implications, *J. Geophys. Res.*, 97(B4), 4995–
5015. 918
919
920
Lin, A. (2007), *Fossil Earthquakes: The Formation and Preservation of*
Pseudotachylytes, 348 pp., Springer, Berlin, Germany. 921
922
Lowe, D. R. (1975), Water escape structures in coarse-grained sediments,
Sedimentology, 22(2), 157–204. 923
924
Magloughlin, J. F. (1992), Microstructural and chemical-changes associated
with cataclasis and frictional melting at shallow crustal levels—The cata-
clastic pseudotachylyte connection, Tectonophysics, 204(3–4), 243–260. 925
926
927

- 928 Magloughlin, J. F., and J. G. Spray (1992), Frictional melting processes
929 and products in geological-materials—Introduction and discussion, *Tec-*
930 *tonophysics*, 204(3-4), 197–206.
- 931 Major, J. J., and T. C. Pierson (1992), Debris flow rheology: Experimental
932 analysis of fine-grained slurries, *Water Resour. Res.*, 28(3), 841–857.
- 933 Maltman, A. (1994), Introduction and overview, in *The Geological Deform-*
934 *ation of Sediments*, edited by A. Maltman, pp. 1–35, Chapman and
935 Hall.
- 936 Mastin, L. G., and M. S. Ghiorso (2000), A numerical program for steady-
937 state flow of magma gas mixtures through vertical eruptive conduits, *U.S.*
938 *Geol. Surv. Open File Rep.* 00-209.
- 939 Meneghini, F., et al. (2007), Unraveling seismic deformation in exhumed
940 subduction thrusts: The ultrafine-grained fault rocks of Pasagshak Point,
941 Kodiak Island, AK (abstracts with programs), *Geol. Soc. Am.*, 39, 374.
- 942 Meneghini, F., et al. (2008), Picturing the seismic cycle along ancient
943 decollement thrusts: The ultrafine-grained fault rocks of Pasagshak Point,
944 Kodiak Island, AK, *Trab. Geol.*, in press.
- 945 Mikaelian, K. O. (1996), Rayleigh-Taylor instability in finite-thickness
946 fluids with viscosity and surface tension, *Phys. Rev. E: Stat. Phys.*,
947 *Plasmas, Fluids, Relat. Interdiscip. Top.*, 54, 3676–3680.
- 948 Nielsen, S., et al. (2008), Frictional melt and seismic slip, *J. Geophys. Res.*,
949 113, B01308, doi:10.1029/2007JB005122.
- 950 Otsuki, K., et al. (2003), Fluidization and melting of fault gouge during
951 seismic slip: Identification in the Nojima fault zone and implications for
952 focal earthquake mechanisms, *J. Geophys. Res.*, 108(B4), 2192,
953 doi:10.1029/2001JB001711.
- 954 Owen, G. (1987), Deformation processes in unconsolidated sands, *Geol.*
955 *Soc. Lond. Spec. Publ.*, 29(1), 11.
- 956 Owen, G. (1996), Experimental soft-sediment deformation: Structures
957 formed by the liquefaction of unconsolidated sands and some ancient
958 examples, *Sedimentology*, 43(2), 279–293.
- 959 Plafker, G., et al. (1994), Geology of the southern Alaska margin, in *The*
960 *Geology of Alaska, The Geology of North America*, edited by G. Plafker
961 and H. C. Berg, pp. 389–449, Geol. Soc. of Am., Boulder, Colo.
- 962 Potter, P. E., and F. J. Pettijohn (1977), *Paleocurrents and Basin Analysis*,
963 2nd ed., Springer-Verlag, New York.
- 964 Rice, J. R. (2006), Heating and weakening of faults during earthquake slip,
965 *J. Geophys. Res.*, 111, B05311, doi:10.1029/2005JB004006.
- 966 Ronnlund, P. (1989), Viscosity ratio estimates from natural Rayleigh-Taylor
967 instabilities, *Terra Nova*, 1, 334–348.
- 968 Rowe, C. D. (2007), *Snapshots of the Earthquake Cycle: An Approach to*
969 *Subduction Zone Paleo-Seismicity*, 185 pp., UC Santa Cruz, Santa Cruz,
970 Calif.
- 971 Rowe, C. D., et al. (2005), Large-scale pseudotachylites and fluidized
972 cataclasites from an ancient subduction thrust fault, *Geology*, 33,
973 937–940.
- Sample, J., and D. Fisher (1986), Duplex accretion and underplating in an 974
ancient accretionary complex, Kodiak Islands, Alaska, *Geology*, 14, 975
160–163. 976
- Shaw, H. (1972), Viscosities of magmatic silicate liquids; an empirical 977
method of prediction, *Am. J. Sci.*, 272, 870–898. 978
- Sibson, R. H., and V. G. Toy (2006), The habitat of fault-generated 979
pseudotachylite: Presence vs. absence of friction-melt, in *Earthquakes:*
980 *Radiated Energy and the Physics of Faulting*, edited by R. Abercrombie
981 et al., AGU, Washington, D. C. 982
- Smith, R. B. (1977), Formation of folds, boudinage, and mullions in non- 983
Newtonian materials, *Geol. Soc. Am. Bull.*, 88, 312–320. 984
- Sonder, L., et al. (2006), Non-Newtonian viscosity of basaltic magma, 985
Geophys. Res. Lett., 33, L02303, doi:10.1029/2005GL024240. 986
- Song, C., et al. (2008), A phase diagram for jammed matter, *Nature*, 987
453(7195), 629–632. 988
- Spray, J. G. (2005), Evidence for melt lubrication during large earthquakes, 989
Geophys. Res. Lett., 32, L07301, doi:10.1029/2004GL022293. 990
- Turcotte, D. L., and G. Schubert (2002), *Geodynamics*, 2nd ed., Cambridge 991
Univ. Press, New York. 992
- Twiss, R. J., and E. M. Moores (1992), *Structural Geology*, W. H. Freeman, 993
New York. 994
- Ujii, K., et al. (2007a), Fluidization of granular material in a subduction 995
thrust at seismogenic depths, *Earth Planet. Sci. Lett.*, 259, 307–318. 996
- Ujii, K., et al. (2007b), Pseudotachylites in an ancient accretionary 997
complex and implications for melt lubrication during subduction zone 998
earthquakes, *J. Struct. Geol.*, 29, 599–613. 999
- Visher, G. S., and R. D. Cunningham (1981), Convolute laminations—a 1000
theoretical analysis: Example of Pennsylvanian sandstone, *Sed. Geol.*, 28,
1001 175–188. 1002
- Vrolijk, P., et al. (1988), Warm fluid migration along tectonic melanges in 1003
the Kodiak accretionary complex, Alaska, *J. Geophys. Res.*, 93(B9), 1004
10,313–10,324. 1005
- Wenk, H. R., et al. (2000), Pseudotachylites in the eastern peninsular ranges 1006
of California, *Tectonophysics*, 321(2), 253–277. 1007
- Wilcock, W. S. D., and J. A. Whitehead (1991), The Rayleigh-Taylor 1008
instability of an embedded layer of low-viscosity fluid, *J. Geophys.*
1009 *Res.*, 96(B7), 12,193–12,200. 1010
- Yuan, F., and V. Prakash (2008), Slip weakening in rocks and analog 1011
materials at co-seismic slip rates, *J. Mech. Phys. Solids*, 56(2), 542–560. 1012
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