Effect of fluid–sediment reaction on hydrothermal fluxes of major elements, eastern flank of the Juan de Fuca Ridge

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Abstract—On the eastern flank of the Juan de Fuca Ridge, reaction between upwelling basement fluid and sediment alters hydrothermal fluxes of Ca, SiO$_2(aq)$, SO$_4$2-, PO$_4$3-, NH$_4$+, and alkalinity. We used the Global Implicit Multicomponent Reactive Transport (GIMRT) code to model the processes occurring in the sediment column (diagenesis, sediment burial, fluid advection, and multicomponent diffusion) and to estimate net seafloor fluxes of solutes. Within the sediment section, the reactions controlling the concentrations of the solutes listed above are organic matter degradation via SO$_4$ reduction, dissolution of amorphous silica, reductive dissolution of amorphous Fe(III)-(hydr)oxide, and precipitation of calcite, carbonate fluorapatite, and amorphous Fe(II)-sulfide. Rates of specific discharge estimated from pore-water Mg profiles are 2 to 3 mm/yr. At this site the basement hydrothermal system is a source of NH$_4$+, SiO$_2(aq)$, and Ca, and a sink of SO$_4$2-, PO$_4$3-, and alkalinity. Reaction within the sediment column increases the hydrothermal sources of NH$_4$ and SiO$_2(aq)$, increases the hydrothermal sinks of SO$_4$ and PO$_4$, and decreases the hydrothermal source of Ca. Reaction within the sediment column has a spatially variable effect on the hydrothermal flux of alkalinity.

Because the model we used was capable of simulating the observed pore-water chemistry by using mechanistic descriptions of the biogeochemical processes occurring in the sediment column, it could be used to examine the physical controls on hydrothermal fluxes of solutes in this setting. Two series of simulations in which we varied fluid flow rate (1 to 100 mm/yr) and sediment thickness (10 to 100 m) predict that given the reactions modeled in this study, the sediment section will contribute most significantly to fluxes of SO$_4$ and NH$_4$ at slow flow rates and intermediate sediment thickness and to fluxes of SiO$_2(aq)$ at slow flow rates and large sediment thickness. Reaction within the sediment section could approximately double the hydrothermal sink of PO$_4$ over a range of flow rates and sediment thickness, and could slightly decrease (by $\pm 10\%$) the size of the hydrothermal source of Ca.

1. INTRODUCTION

The contribution of hydrothermal circulation through mid-ocean ridge crests and ridge flanks to the oceanic mass balance of some elements is comparable to the riverine contribution (Kadko et al., 1995). Although the composition of low-temperature hydrothermal fluids found on ridge flanks differs less from seawater than does that of high-temperature ridge-crest fluids, the larger volume of fluid that circulates through ridge flanks suggests that they may provide a similar or larger source or sink of several elements, including Mg, Ca, Si, and P (Mottl and Wheat, 1994; Kadko et al., 1995; Tréguer et al., 1995; Wheat et al., 1996). In ridge-flank environments a portion of the fluid entering and exiting the crust passes through the sediment section (e.g., Williams et al., 1979; Maris and Bender, 1982; Bender et al., 1985; Mottl, 1989; Wheat and McDuff, 1994, 1995; Wheat and Mottl, 1994; Davis et al., 1997; Fisher et al., 2001). Estimates of ridge-flank geochemical fluxes are derived from basement pore-water compositions (e.g., Wheat and Mottl, 2000) or from an accounting of basement alteration products (e.g., Alt and Teagle, 1999) and thus do not account for the influence of reactions within the sediment column on solute fluxes. In this article, we evaluate the effect of reaction between upwelling, basement-derived hydrothermal fluid and sediment on fluxes of Ca, SiO$_2$, SO$_4$, PO$_4$, NH$_4$, and alkalinity for two sites on the eastern flank of the Juan de Fuca Ridge.

Most studies of fluid advection through ridge flank sediments have used pore-water geochemical profiles to estimate flow rates and to identify reactions occurring in the sediment but have not attempted to quantify the influence of sediment diagenesis on hydrothermal fluid composition or vice versa. Exceptions include the diagenetic models of Wheat and McDuff (1994) and Wheat and Tribble (1994), which showed that upwelling hydrothermal fluids enhance amorphous silica dissolution and organic carbon degradation in the Marianas Mounds and result in the early transformation of amorphous silica to quartz in Middle Valley. In studies of sediment mineralogy, other effects of basement-derived hydrothermal fluid on sediment diagenesis have been documented, including early formation of chalcedony (Kastner et al., 1986) and replacement of calcareous–siliceous ooze with authigenic clays and oxides (Williams et al., 1979). These models and observations suggest that the reaction of upwelling, basement-derived hydrothermal fluid with sediment results in hydrothermal fluxes of solutes to and from the ocean that differ from the fluxes that result when basement fluid bypasses the sediment section.

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We used sediment pore-water geochemical data from Ocean Drilling Program (ODP) sites 1030 and 1031 (Davis et al., 1997; Mottl et al., 2000) to constrain a coupled reactive transport model of processes occurring in the sediment column. We included a full suite of major seawater species and a set of diagenetic reactions that are stoichiometrically consistent and whose rates of reaction are controlled by thermodynamic and kinetic constants. Because the model simulated the reaction mechanisms by which fluid composition changes, it could be used to evaluate the parameters controlling solute fluxes. We varied fluid flow rate and sediment thickness to determine the range of each over which upward seepage of hydrothermal fluid through sediment alters hydrothermal fluxes. With respect to this emphasis on understanding the mechanisms that control sediment pore-water geochemistry, our study is similar to models of early diagenesis that seek to understand the processes controlling diffusive fluxes and burial fluxes of, for instance, P (Van Cappellen and Berner, 1988), SiO$_2$$_{\text{aq}}$ (Raboulille et al., 1997), or Fe and Mn (Van Cappellen and Wang, 1996; Wang and Van Cappellen, 1996).

2. JUAN DE FUCA RIDGE FLANK

The Juan de Fuca Ridge lies several hundred kilometers west of the North American continent (Fig. 1). A landward-thickening blanket of interbedded turbidites and hemipelagic clay deposited primarily during Pleistocene glaciation onlaps basalt 20 km east of the spreading center (Davis et al., 1997). Upward seepage of basement hydrothermal fluid through sediment occurs above a small basement high 40 km east of the spreading center (Wheat and Mottl, 1994; Davis et al., 1997). Uplift rates based on curvature in pore-water profiles of conservative elements range from 0.07 to 3.2 mm/yr (specific discharge) (Wheat and Mottl, 1994; Davis et al., 1997; this work).

Sediments at ODP sites 1030 and 1031 are hemipelagic clays and silts with interbedded silty turbidites. They contain calcite (2 to 40 wt% dry), phyllosilicates (30 to 50%), quartz (5 to 30%), feldspar (10 to 30%), pyrite (2 to 10%), and organic carbon (0.2 to 0.6%) (Davis et al., 1997). The sediment column maintains 60 to 80% porosity (average ~70%) throughout its thickness. Sedimentation rate has varied from 3 to 17 cm/ka and averages 4 to 6 cm/ka (Davis et al., 1997). Temperatures at the sediment–basement interface are 40.1°C and 40.4°C at ODP sites 1030 and 1031, respectively (Davis et al., 1997). Seepage rates are not fast enough to disturb linear thermal gradients.

The extensive pore-water geochemistry data set from ODP sites 1030 and 1031 includes concentrations of major seawater species, alkalinity, nutrients, and minor species such as Fe and F (Davis et al., 1997; Mottl et al., 2000) whose concentrations help constrain reactions affecting alkalinity and major species. At both sites pore-water samples were collected at 1.5- to 9.5-m intervals from 1.45 m below the seafloor (mbsf) to the base of the cored sediment section (5 m above the sediment–basement interface (41.7 mbsf) at ODP site 1030 and the sediment–basement interface (41.3 mbsf) at ODP site 1031) (Davis et al., 1997).

Pore fluids at the base of the sediment column are depleted in alkalinity, SO$_4$, and PO$_4$, and enriched in NH$_4$, Ca, and SiO$_2$, relative to bottom seawater (Davis et al., 1997). The pore fluid composition is similar to that of 64°C basement water collected 60 km to the east (Davis et al., 1997) and to that of hydrothermal fluid collected at warm springs on the Baby Bare basement outcrop, also located ~60 km to the east (Mottl et al., 1998; Wheat and Mottl, 2000). The similarities suggest that hydrothermal fluids at ODP sites 1030 and 1031 equilibrated with basement at a similarly high temperature (Davis et al., 1997; Elderfield et al., 1999) and that the site can be categorized as a “warm” (>45°C) hydrothermal site (Mottl and Wheat, 1994).

Warm sites have been discovered only on young (<6 Ma), rapidly sedimented crust, but reaction of seawater with basalt at warm sites could remove the entire river input of Mg if such sites account for only 8 to 20% of the total advective heat loss on ridge flanks (Wheat and Mottl, 1994). On the basis of the assumption that they remove 100% of river Mg, the composition of Baby Bare spring water suggests that warm sites could provide a source of Ca to the ocean as large as 39% of the river input and remove as much as 34% of the river input of SO$_4$ (Table 1) (Wheat and Mottl, 2000). Although ridge-flank hy-
Table 1. Estimated global fluxes from warm ridge-flank hydrothermal sites.

<table>
<thead>
<tr>
<th>Species</th>
<th>Baseline hydrothermal fluxa</th>
<th>Sediment hydrothermal fluxb</th>
<th>River input (mol/yr)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>mol/yr</td>
<td>% river input</td>
<td>mol/yr</td>
</tr>
<tr>
<td>SO₄⁻</td>
<td>7.9E+09</td>
<td>0.3</td>
<td>2.1E+10</td>
</tr>
<tr>
<td>NH₄⁺</td>
<td>1.8E+10</td>
<td>0.4</td>
<td>2.2E+11</td>
</tr>
<tr>
<td>SiO₂</td>
<td>4.7E+12</td>
<td>39</td>
<td>4.2E+12</td>
</tr>
<tr>
<td>PO₄³⁻</td>
<td>-2.6E+08</td>
<td>-0.3</td>
<td>-4.8E+08</td>
</tr>
<tr>
<td>Alkalinity</td>
<td>-2.4E+11</td>
<td>-0.7</td>
<td>-1.9E+11</td>
</tr>
</tbody>
</table>

a Derived from Baby Bare spring water composition with the assumption that warm ridge-flank hydrothermal sites remove the entire river input of Mg (Sansone et al., 1998; Wheat and Mottl, 2000). The flux of NH₄⁺ was calculated for this study by means of the method and data of Wheat and Mottl (2000).

b Basement hydrothermal flux multiplied by the ratio $F_{so}/F_{H}$ obtained in simulations of ODP site 1030 (Table 8).

c Wheat and Mottl (2000).
d Total dissolved N (Jickells, 1995).
e Tréguer et al. (1995).
f Wheat et al. (1996).
g Berner et al. (1983).

drothermal circulation (at all temperatures) may remove as much as 21% of river input of PO₄ (Wheat et al., 1996) and contribute up to 36% of river SiO₂$_{aq}$ (Kadko et al., 1995). Baby Bare spring water composition suggests that much as 21% of river input of PO₄ (Wheat et al., 1996) and SiO₂$_{aq}$ (Kadko et al., 1995) to model the steady-state interaction of sediment burial, fluid advection, molecular diffusion, organic matter degradation (via O₂ respiration and SO₄ reduction), and inorganic mineral diagenesis occur. Aqueous species included in the model are major seawater solutes and several minor solutes of importance to mineral diagenesis (Table 2). Reactive solid phases included in the model are organic matter, calcite, carbonate fluorapatite (CARFAP), solid iron hydroxide (Fe(OH)$_3$(s)), amorphous iron sulfide (FeS$_{am}$b), and biogenic amorphous silica (SiO₂$_{am}$). Associated reactions (Table 3) are described in Section 3.2.

3. MODELING METHODS

We used an updated version of the numerical code Global Implicit Multicomponent Reactive Transport (GIMRT) (Steefel and Yabusaki, 1996; Steefel, 2000) to model the steady-state interaction of sediment and hydrothermal fluid in a one-dimensional domain within which sediment burial, fluid advection, molecular diffusion, organic matter degradation (via O₂ respiration and SO₄ reduction), and inorganic mineral diagenesis occur. Aqueous species included in the model are major seawater solutes and several minor solutes of importance to mineral diagenesis (Table 2). Reactive solid phases included in the model are organic matter, calcite, carbonate fluorapatite (CARFAP), solid iron hydroxide (Fe(OH)$_3$(s)), amorphous iron sulfide (FeS$_{am}$b), and biogenic amorphous silica (SiO₂$_{am}$). Associated reactions (Table 3) are described in Section 3.2.

3.1. Model Architecture

GIMRT solves the nonlinear set of partial differential equations describing coupled reaction and transport by using finite volume techniques (Steefel and Lasaga, 1994; Steefel and Lichtner, 1994, 1998; Steefel and Yabusaki, 1996; Steefel, 2000). Aqueous, surface complexation, and ion exchange reactions are formulated in this problem as equilibrium reactions. Mineral dissolution and precipitation and oxidation reduction (redox) reactions are formulated as rate-controlled reactions. GIMRT provides several rate laws options, including rate laws based on transition state theory for mineral dissolution and precipitation (e.g., Lasaga, 1998) and multiplicative Monod kinetics for organic matter degradation (e.g., Wittmann and Van Briesen, 1996; Van Cappellen and Gaillard, 1996). Although GIMRT has been used previously to simulate reactive transport problems in which molecular diffusion was either dominant (Steefel and Lichtner, 1994) or important (Steefel and Lichtner, 1998; Steefel, 2000), for this study the code has been modified to allow the use of species-specific diffusion coefficients.

3.1.1. Mass Conservation

Mass conservation is maintained on total concentrations of “primary species,” a user-specified set of species that provides a complete stoichiometric formula for each species in the system. “Secondary species” are those involved in equilibrium reactions (including sorption) with the primary species. Because concentrations of secondary species can be expressed algebraically in terms of primary species concentrations, separate mass conservation equations are not required (Morel and Hering, 1993; Steefel and MacQuarrie, 1996). The total concentration ($T_j$) of a primary species is expressed as

$$T_j = C_j + \sum_{i=1}^{Nt} v_{j,i} C_i,$$

where $C_j$ is the concentration of primary species $j$ (mol/kg water), $N_t$ is the total number of secondary species in the system, $v_{j,i}$ is the stoichiometric coefficient for the secondary species (i.e., the number of moles of primary species $j$ in secondary species $i$), and $C_i$ is the concentration of secondary species $i$. The change in $T_j$ with time is given by:

$$\frac{\partial}{\partial t} \phi \rho T_j = \frac{\partial}{\partial x} \left( J_{p,j}^r + J_{p,j}^d \right) + \sum_{i=1}^{N_t} v_{j,i} R_{j,i},$$

where $\phi$ is the porosity and $\rho$ is the fluid density. The first term on the right-hand side accounts for advective ($J_{p,j}^r$) and diffusive ($J_{p,j}^d$) fluxes ($x$ represents depth). The second term on the right-hand side accounts for production and consumption due to kinetically controlled reactions, where $N_r$ is the number of kinetically controlled reactions, $R_i$ is the reaction rate of the $r$th reaction pathway (units of moles per m$^2$ porosity per unit time), and $v_{j,i}$ is the stoichiometric coefficient of primary species $j$ in the $r$th reaction. Although Eqn. 2 is written in terms of total concentration, GIMRT solves for individual concentrations of primary species and thus effectively folds a speciation calculation into the solution of the governing differential equations (Steefel and Lasaga, 1994).

Conservation equations written in terms of total concentrations of primary species are used in many geochemical (e.g., Morel and Hering, 1993; Parkhurst, 1995) and reactive transport (e.g., Yeh and Tripathi, 1989; Lichtner, 1992, 1996; Steefel and Lasaga, 1994) models, because the formulation allows arbitrary combinations of equilibrium and kinetic reactions provided each species involved in a kinetically controlled reaction is considered a primary species (Steefel and MacQuarrie, 1996). For example, because we consider redox reactions...
3.1.2. Advective Flux

The advective flux of a primary species ($J_i^\text{tot}$ in Eqn. 2) is the sum of the fluxes of dissolved and sorbed species contributing to $T_i^\text{sp}$. Sorbed species (like minerals) are transported only by burial, which is treated as a standard advection term (Berner, 1980). This portion of $J_i^\text{tot}$ is given by:

$$\dot{J}_i^\text{sp} = \omega \Phi \rho T_i^\text{sp},$$

(3)

where $\omega$ is the burial rate and $T_i^\text{sp}$ is the portion of $T_i$ accounted for by sorbed species (in mol/kg water). The advective flux of a dissolved species includes both fluid flow and burial. This portion of $J_i^\text{tot}$ is given by:

$$\dot{J}_i^\text{diss} = \omega \Phi \rho T_i^\text{diss} + p q T_i^\text{dis},$$

(4)

where $T_i^\text{diss}$ is the portion of $T_i$ accounted for by dissolved species, and $q$ is specific discharge. Sediment compaction is neglected.

3.1.3. Diffusive Flux

The version of GIMRT used in this work is the first to incorporate species-specific diffusion coefficients, which are necessary to capture the behavior of a system, such as that considered here, in which diffusive transport plays an important role. A rigorous treatment of multicomponent diffusion has been widely described in the sediment diagenesis literature (e.g., Lasaga, 1979, 1998; McDuff and Ellis, 1979; Van Cappellen and Gaillard, 1996), although simpler treatments are more commonly implemented (e.g., Boudreau and Canfield, 1993; Van Cappellen and Wang, 1996). Rigorous treatment requires that diffusive fluxes be written in terms of gradients in chemical potential rather than concentration. Doing so introduces gradients in activity coefficients and an electrochemical migration term that maintains electrical neutrality at the macroscopic scale (Lichtner, 1996; Van Cappellen and Gaillard, 1996). For our simulations, gradients in activity coefficients are negligible, because ionic strength is nearly constant and temperature gradients are small. Neglecting gradients in activity coefficients, the diffusive flux of an individual species in one dimension is given by:

$$J_i = -D_i^\text{mm} \left[ \frac{\partial C_i}{\partial x} - \sum_{j=1}^{n_s} z_i z_j C_j D_{ij} \frac{\partial C_j}{\partial x} \right]$$

(5)

where $D_i^\text{mm}$ is the porous-medium diffusion coefficient for species $i$, $z_i$ is the charge of species $i$, and $N_s$ is the total number of species in the system. The first term on the right-hand side represents the Fickian component of the diffusive flux; the second accounts for electrochemical migration (Van Cappellen and Gaillard, 1996). The total diffusive flux of a primary species ($J_i^\text{mm}$ in Eqn. 2) is obtained by summing diffusive fluxes for all species contributing to $T_i$ (see Appendix). The electrochemical migration term vanishes if diffusion coefficients for all

<table>
<thead>
<tr>
<th>Species</th>
<th>Seawater$^a$</th>
<th>1030B</th>
<th>1031A</th>
</tr>
</thead>
<tbody>
<tr>
<td>CO$_2$(aq)</td>
<td>$2.37 \times 10^{-3}$</td>
<td>$3.76 \times 10^{-5}$</td>
<td>$4.17 \times 10^{-5}$</td>
</tr>
<tr>
<td>NH$_4$</td>
<td>$3.0 \times 10^{-7}$</td>
<td>$2.06 \times 10^{-4}$</td>
<td>$1.00 \times 10^{-4}$</td>
</tr>
<tr>
<td>Mg</td>
<td>$5.2 \times 10^{-2}$</td>
<td>$5.68 \times 10^{-3}$</td>
<td>$4.65 \times 10^{-3}$</td>
</tr>
<tr>
<td>Ca</td>
<td>$1.03 \times 10^{-2}$</td>
<td>$5.71 \times 10^{-2}$</td>
<td>$6.02 \times 10^{-2}$</td>
</tr>
<tr>
<td>K</td>
<td>$1.01 \times 10^{-2}$</td>
<td>$6.41 \times 10^{-3}$</td>
<td>$6.56 \times 10^{-3}$</td>
</tr>
<tr>
<td>SO$_4$</td>
<td>$2.81 \times 10^{-2}$</td>
<td>$2.23 \times 10^{-2}$</td>
<td>$2.34 \times 10^{-2}$</td>
</tr>
<tr>
<td>H$_2$PO$_4$</td>
<td>$2.8 \times 10^{-6}$</td>
<td>$1.3 \times 10^{-8}$</td>
<td>$2.0 \times 10^{-8}$</td>
</tr>
<tr>
<td>SiO$_2$(aq)</td>
<td>$1.9 \times 10^{-4}$</td>
<td>$2.21 \times 10^{-4}$</td>
<td>$2.57 \times 10^{-4}$</td>
</tr>
<tr>
<td>Na</td>
<td>$4.66 \times 10^{-1}$</td>
<td>$4.705 \times 10^{-1}$</td>
<td>$4.684 \times 10^{-1}$</td>
</tr>
<tr>
<td>Cl</td>
<td>$5.42 \times 10^{-1}$</td>
<td>$5.577 \times 10^{-1}$</td>
<td>$5.577 \times 10^{-1}$</td>
</tr>
<tr>
<td>H$_2$S(aq)</td>
<td>$1.0 \times 10^{-15}$</td>
<td>$1.57 \times 10^{-7}$</td>
<td>$8.97 \times 10^{-7}$</td>
</tr>
<tr>
<td>Fe$^{II}$</td>
<td>$6.0 \times 10^{-10}$</td>
<td>$3.3 \times 10^{-6}$</td>
<td>$7.0 \times 10^{-6}$</td>
</tr>
<tr>
<td>Mn$^{II}$</td>
<td>$5.0 \times 10^{-10}$</td>
<td>$3.18 \times 10^{-5}$</td>
<td>$9.0 \times 10^{-6}$</td>
</tr>
<tr>
<td>B(OH)$_3$(aq)</td>
<td>$4.1 \times 10^{-4}$</td>
<td>$4.12 \times 10^{-4}$</td>
<td>$3.29 \times 10^{-4}$</td>
</tr>
<tr>
<td>F</td>
<td>$3.85 \times 10^{-5}$</td>
<td>$1.71 \times 10^{-5}$</td>
<td>$8.4 \times 10^{-6}$</td>
</tr>
<tr>
<td>O$_2$(aq)</td>
<td>$1.80 \times 10^{-48}$</td>
<td>$1.0 \times 10^{-15}$</td>
<td>$1.0 \times 10^{-15}$</td>
</tr>
<tr>
<td>NO$_3$</td>
<td>$3.92 \times 10^{-5}$</td>
<td>$1.0 \times 10^{-6}$</td>
<td>$1.0 \times 10^{-6}$</td>
</tr>
</tbody>
</table>

Table 2. Primary species and boundary condition total concentrations, alkalinity, and pH.

<table>
<thead>
<tr>
<th>Total concentration (mol/kg)</th>
<th>Basement water$^b$</th>
</tr>
</thead>
<tbody>
<tr>
<td>pH</td>
<td>7.9</td>
</tr>
<tr>
<td>Alkalinity (Eq/kg)</td>
<td>4.6 $\times 10^{-4}$</td>
</tr>
<tr>
<td>9 $\times 10^{-4}$</td>
<td>8.55$^m$</td>
</tr>
<tr>
<td>8.46$^m$</td>
<td></td>
</tr>
</tbody>
</table>

$^a$ Measured at Baby Bare (Wheat and Mottl, 2000) unless otherwise noted.

$^b$ Concentration in deepest pore fluid sample unless otherwise noted.

$^c$ Constrained by charge balance.

$^d$ Assumed to be all Fe(II) and Mn(II).

$^e$ Independent parameter in model, but constrained by measured alkalinity and pH.

$^f$ Arbitrary, essentially 0 mol/kg.

$^g$ Concentration in shallowest pore fluid sample from ODP site 1030.

$^h$ In equilibrium with CaCO$_3$.

$^i$ In equilibrium with CARFAP.

$^j$ In equilibrium with FeS$_{FeS(II)}$.

$^k$ Baby Bare spring water (Wheat and Mottl, 2000).

$^l$ Not an independent condition.

kinetically controlled, each redox state of a particular element (e.g., S(II) and S(VI)) requires definition of a different primary species (e.g., H$_2$S and SO$_4^{2-}$).

3.1.2. Advective Flux

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(5)

where $D_i^\text{mm}$ is the porous-medium diffusion coefficient for species $i$, $z_i$ is the charge of species $i$, and $N_s$ is the total number of species in the system. The first term on the right-hand side represents the Fickian component of the diffusive flux; the second accounts for electrochemical migration (Van Cappellen and Gaillard, 1996). The total diffusive flux of a primary species ($J_i^\text{mm}$ in Eqn. 2) is obtained by summing diffusive fluxes for all species contributing to $T_i$ (see Appendix). The electrochemical migration term vanishes if diffusion coefficients for all
aqueous species in the system are the same. The inclusion of this term in the case of unequal diffusion coefficients introduces a slight curvature into what would otherwise be a linear profile of a conservative ion undergoing pure diffusive transport at steady state.

We modeled diffusion of the primary and secondary species that contributed the most to mass balance calculations by using temperature-dependent, species-specific diffusion coefficients, measured in seawater or corrected for the viscosity of seawater (Table 4) (Wollast and Garrels, 1971; Li and Gregory, 1974; Boudreau and Canfield, 1993). For all other species we used a temperature-dependent diffusion coefficient with a value at 25°C of 0.9 × 10⁻⁵ m²/s. Temperature dependence was calculated from the Arrhenius equation (Lasaga, 1998) by using an activation energy of 19 kJ/mol. We calculated diffusion coefficients appropriate for a porous medium according to (McDuff and Ellis, 1979):

\[ D'_{\text{corr}} = \frac{D'}{\phi F} \]  

where \( D' \) is the temperature-corrected diffusion coefficient in the fluid, \( \phi \) is porosity (equal to 0.7), and \( F \) is formation factor (equal to 3) (Davis et al., 1997).

### 3.1.4. Equilibrium Constants

GIMRT employs true thermodynamic equilibrium constants (functions of temperature and pressure only) and calculates species activities by using the extended Debye–Hückel formula with an additional correction for ionic strength (the B-dot formulation) and temperature-dependent constants (Helgeson, 1969; Johnson et al., 1992). This

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**Table 3. Heterogeneous reactions and their kinetic constants, seafloor concentrations, and reactive surface areas of solid phases.**

<table>
<thead>
<tr>
<th>Phase</th>
<th>Reaction stoichiometry</th>
<th>log ( k^b ) (kJ/mol)</th>
<th>( K_{\text{act}} ) (mol/kg)</th>
<th>Concentration</th>
<th>Area ( ^a ) (m²/m³ bulk)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Organic for ( \text{O}_2 \text{(aq)} )</td>
<td>((\text{CH}_3\text{O})_3\text{Na}(\text{HPO}_4)^- + 1380\text{H}_2\text{O} \rightarrow 106\text{CO}_2\text{(aq)} + )</td>
<td>-10.51</td>
<td>0</td>
<td>2 × 10⁻⁵</td>
<td>1420</td>
</tr>
<tr>
<td>Minerals</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Calcite</td>
<td>( \text{CaCO}_3 + \text{H}^+ \rightarrow \text{Ca}^{2+} + \text{HCO}_3^- )</td>
<td>-6.19</td>
<td>63</td>
<td>NA</td>
<td>0.05</td>
</tr>
<tr>
<td>CARFAP</td>
<td>( \text{Ca}_3(\text{PO}<em>4)</em>{2.45}(\text{CO}<em>3)</em>{0.65} \cdot \text{H}_2\text{O} \rightarrow 10\text{Ca}^{2+} + 4.975\text{PO}_4^{3-} + )</td>
<td>-10</td>
<td>47</td>
<td>NA</td>
<td>0</td>
</tr>
<tr>
<td>SiO(_2\text{(am)})</td>
<td>( \text{SiO}_2(\text{am}) + 3\text{H}_2\text{O} \rightarrow \text{SiO}_2(\text{am}) + 6\text{OH}^- )</td>
<td>-11.2</td>
<td>63</td>
<td>NA</td>
<td>0.004</td>
</tr>
<tr>
<td>Fe(_2\text{(am)})</td>
<td>( \text{FeS}_{(am)} + \text{H}^+ \rightarrow \text{Fe}^{2+} + \text{HS}^- )</td>
<td>-9</td>
<td>0</td>
<td>NA</td>
<td>0</td>
</tr>
<tr>
<td>Fe(\text{OH})(_3\text{(am)})</td>
<td>( \text{Fe(OH)}_3(\text{am}) + 0.5\text{H}_2\text{O} \rightarrow \text{Fe}^{3+} + \text{H}_2\text{O} + 2\text{OH}^- + 0.5\text{Si}^{4+} - 4.99\text{m}^3/\text{s}</td>
<td>4.5</td>
<td>NA</td>
<td>0.004</td>
<td>0.29</td>
</tr>
</tbody>
</table>

**Table 4. Species-specific diffusion coefficients at 25°C.**

<table>
<thead>
<tr>
<th>Cations</th>
<th>( D' ) (m²/s)</th>
<th>Anions</th>
<th>( D' ) (m²/s)</th>
<th>Neutral species</th>
<th>( D' ) (m²/s)</th>
</tr>
</thead>
<tbody>
<tr>
<td>\text{H}^+</td>
<td>8.57E – 09</td>
<td>\text{OH}^-</td>
<td>4.85E – 09</td>
<td>\text{CO}_2\text{(aq)}</td>
<td>1.76E – 09</td>
</tr>
<tr>
<td>\text{Na}^+</td>
<td>1.22E – 09</td>
<td>\text{Cl}^-</td>
<td>1.87E – 09</td>
<td>\text{H}_2\text{SiO}_4\text{(aq)}</td>
<td>1.79E – 09</td>
</tr>
<tr>
<td>\text{K}^+</td>
<td>1.80E – 09</td>
<td>\text{F}^-</td>
<td>1.34E – 09</td>
<td>\text{NH}_3\text{(aq)}</td>
<td>2.07E – 09</td>
</tr>
<tr>
<td>\text{Mg}^{2+}</td>
<td>6.49E – 10</td>
<td>\text{HCO}_3^-</td>
<td>1.09E – 09</td>
<td>\text{B(OH)}_3\text{(aq)}</td>
<td>1.11E – 09</td>
</tr>
<tr>
<td>\text{Ca}^{2+}</td>
<td>7.30E – 10</td>
<td>\text{CO}_3^{2-}</td>
<td>8.79E – 10</td>
<td>\text{B(OH)}_2</td>
<td>9.70E – 10</td>
</tr>
<tr>
<td>\text{Fe}^{2+}</td>
<td>6.61E – 10</td>
<td>\text{HSO}_4^-</td>
<td>1.12E – 09</td>
<td>\text{SiO}_2\text{(aq)}</td>
<td>1.00E – 09</td>
</tr>
<tr>
<td>\text{NH}_4^+</td>
<td>1.82E – 09</td>
<td>\text{SO}_4^{2-}</td>
<td>9.84E – 10</td>
<td>\text{O}_2\text{(aq)}</td>
<td>2.08E – 09</td>
</tr>
<tr>
<td>\text{Mn}^{2+}</td>
<td>6.33E – 10</td>
<td>\text{HS}^-</td>
<td>1.59E – 09</td>
<td>\text{H}_2\text{PO}_4^-</td>
<td>7.78E – 10</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>\text{HPO}_4^{2-}</td>
<td>6.75E – 10</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>\text{PO}_4^{3-}</td>
<td>5.63E – 10</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
<td>\text{NO}_3^-</td>
<td>1.77E – 09</td>
</tr>
</tbody>
</table>

---

\( ^a \) Li and Gregory (1974), corrected for the viscosity of seawater.

\( ^b \) Boudreau and Canfield (1993), corrected for the viscosity of seawater.

\( ^c \) Wollast and Garrels (1971), measured in seawater.
approach is commonly used to model high-temperature aqueous geochemical systems (e.g., Bowers and Taylor, 1985), but the more common approach for low-temperature seawater systems is to correct for the nonideality of the solution by using seawater-specific activity coefficients or equilibrium constants (e.g., Boudreau and Canfield, 1993). Use of seawater-specific constants produces accurate results for seawater systems and reduces the number of aqueous complexes that need to be included in a model to capture the dependence of mineral solubilities on pH and other variables. The thermodynamic approach used by GIMRT, however, allows systems with pore fluid compositions that differ from seawater (such as those investigated in this article) to be modeled.

We used the code SUPCRT (Johnson et al., 1992) to generate thermodynamic equilibrium constants for the approximate pressure at the seafloor (2600 kPa) and a range of temperatures (0 to 70°C) slightly greater than the observed range (2 to 40°C). The SUPCRT-generated database includes temperature-dependent thermodynamic constants for a large number of aqueous complexation, mineral dissolution, and redox reactions. As described in Section 3.2., we augmented the database with stability constants for solid phases not included in the SUPCRT code (Table 5), and with ion exchange and surface complexation equilibrium constants. Our models included 18 primary aqueous species (Table 2) and 59 secondary aqueous species. Including the large number of secondary species allowed accurate description of mineral solubilities under variable temperature and pH conditions and at ambient pressure conditions.

### 3.1.5. Rate Laws

We modeled SO$_4$ reduction and O$_2$ respiration by using multiplicative Monod kinetics (Rittmann and Van Briesen, 1996; Van Cappellen and Gaillard, 1996; Boudreau, 1997):

$$ \text{Rate} = k \frac{I}{T_{\text{OM}}} [\text{OM}], $$

where $k$ is the rate constant (first order with respect to [OM], the concentration of organic matter), $I$ accounts for inhibition of a reaction pathway by an energetically more favored pathway, $T_{\text{OM}}$ is the total concentration of the electron receptor, and $K_{\text{OM}}$ is the half saturation constant (the electron receptor concentration at which the rate becomes half of its maximum value). In simulations that included O$_2$ respiration, the inhibition of SO$_4$ reduction was modeled with a hyperbolic function of the form:

$$ I = \frac{K_{\text{OM}}}{K_{\text{OM}} + T_{\text{OM}}}, $$

where $K_{\text{OM}}$ is the total concentration of O$_2$ above which SO$_4$ reduction is inhibited (1 μmol/kg).

We modeled inorganic mineral precipitation and dissolution reactions by using rate laws based on transition state theory (Lasaga, 1998):

$$ \text{Rate} = A k \left( \prod_{i=1}^{n} \alpha_i^p \right) \left( 1 - \frac{Q}{K} \right), $$

where $A$ is the area of the surface mineral and $k$ is the temperature-dependent, far-from-equilibrium rate constant for dissolution. The term $H_\infty$ gives the far-from-equilibrium dependence on activities of dissolved species: $N_i$ is the total number of species affecting the far-from-equilibrium rate of the reaction, $\alpha_i$ is the activity of species $i$, and $p$ is the empirically determined exponential dependence. Alternatively, $\alpha_i$ may be replaced with $T_i$, the total concentration of a primary species. The term $(1 - Q/K)$, where $Q$ is the ion activity product and $K$ is the thermodynamic constant, is the saturation state of the fluid with respect to the mineral. We calculated the temperature dependence of rate constants by using the Arrhenius equation (Lasaga, 1998) and the activation energies listed in Table 3.

### 3.2. Reaction Network

#### 3.2.1. Organic Matter Degradation

Measured pore-water concentrations of SO$_4$ and NH$_4$ from ODP sites 1030 and 1031 (Fig. 2) indicate that organic matter degradation via microbially mediated SO$_4$ reduction occurs throughout the sampled sections. We modeled this process by using an organic solid phase with the composition (CH$_2$O)$_{106}$ (NH$_3$)$_{16}$ (H$_3$PO$_4$) for the organic material, modified to account for the nonstoichiometric release of PO$_4$ during O$_2$ respiration (Ingall and Van Cappellen, 1990), which probably occurs in the uppermost sediment section. We used measured pore water SO$_4$ and NH$_4$ to constrain the concentration of reactive organic matter entering the model domain and the rate constant for SO$_4$ reduction at each site.

Because we do not have pore-water data from depths <1.45 mbsf at either site, we cannot evaluate the extent to which organic matter degradation occurs via other, energetically more favored pathways. Given the sedimentation rate of 4 to 6 cm/ka, O$_2$ respiration (in the absence of fluid advection) is predicted to consume 90 to 95% of the reactive organic matter deposited on the seafloor (Tromp et al., 1995). At ODP sites 1030 and 1031 O$_2$ respiration may consume less organic matter than predicted on the basis of sedimentation rate, because the advection-enhanced upward flux of reduced species may consume a large amount of O$_2$. We included a generic calculation of O$_2$ respiration in selected runs to qualitatively assess its impact on solute fluxes. We modeled O$_2$ respiration by using an organic solid phase with a Redfield composition, (CH$_2$O)$_{106}$ (NH$_3$)$_{16}$ (H$_3$PO$_4$). This stoichiometry results in a conservative estimate of the ratio of P released to C released, which could be as high as 30:106 during O$_2$ respiration (Ingall and Van Cappellen, 1990). We used the bottom water O$_2$ concentration, rate constant, and reactive organic matter concentration set forth by Ingall and Van Cappellen (1990) as appropriate for most of the ocean floor. The effect of bioturbation on organic matter distribution is implicitly accounted for within the rate constant (necessary because bioturbation...
3.2.2. Calcite

At ODP sites 1030 and 1031 the measured ratio of alkalinity produced to sulfate consumed, which falls below that predicted from organic matter degradation via SO$_4$ reduction, indicates precipitation of a carbonate mineral. Foraminifera and nannofossils, observed throughout the sediment section at ODP sites 1030 and 1031 (Davis et al., 1997), presumably provide nucleation surfaces for the precipitation of authigenic calcite. In some cases, laboratory-measured rates of calcite dissolution have a high-order dependence on saturation state \[(1/Q/K)^3 \text{ to } (1/Q/K)^{11}\] (Morse, 1978; Eisenlohr et al., 1999). We modeled the process by using a linear dependence (Chou et al., 1989), which results in a slower rate far from equilibrium and a faster rate close to equilibrium than obtained with a nonlinear rate law. Either formulation would result in rates of dissolution and precipitation fast enough to keep pore fluids in equilibrium with calcite throughout the model domain.

3.2.3. Carbonate Fluorapatite

At ODP site 1030, the measured F concentrations fall below those predicted by an advective-diffusive model, and the PO$_4$ concentrations are depressed below those predicted by degradation of organic matter with a C:P ratio of 106:0.5. In other marine sediments, similar modifications to F and PO$_4$ profiles have been correlated with precipitation of authigenic CARFAP (Froelich et al., 1983; Jahnke et al., 1983; Ruttenberg and Berner, 1993), which can form as a dispersed phase in clay-rich sediments (Ruttenberg and Berner, 1993).

Experimental studies (Jahnke, 1984) and detailed analyses of authigenic CARFAP (Glenn et al., 1988) demonstrated that as the CO$_3^{2-}$/H$_2$O activity of the solution increases, the ratio of CO$_3$/PO$_4$ in CARFAP and the solubility of CARFAP both increase. Because the carbonate ion activity of ODP site 1030 and 1031 pore fluids remains similar to or less than that of seawater (\[
\text{H}_2\text{O}\]) throughout the sediment column, we chose a CO$_3$/PO$_4$ ratio of 1.5:4.975 and an equilibrium constant at 20°C appropriate for seawater (Jahnke, 1984). We assumed that the temperature dependence of the equilibrium constant for CARFAP was the same as that for fluorapatite, which we calculated by SUPCRT (Johnson et al., 1992) at atmospheric pressure. We chose rate law parameters on the basis of those measured for pure fluorapatite (Van Cappellen and Berner, 1991), but used a linear dependence on saturation state instead of the second order dependence observed for near-equilibrium precipitation of fluorapatite. The linear dependence results in faster rates of CARFAP precipitation than would a second order dependence.
3.2.4. Fe(OH)$_3$(s) and FeS$_{am}$

Low sulfide concentrations in ODP site 1030 and 1031 pore waters (less than a few μmol/kg on the basis of the absence of sulfide odor) and the occurrence of pyrite in sediments indicate the presence of poorly crystalline Fe(III)-(hydr)oxide and Fe-sulfide phases. The reductive dissolution of Fe(III)-(hydr)oxides by $H_2S$, which occurs $\sim 10^3$ times faster than similar reactions involving Fe(III)-silicates, prevents the build up of pore-water sulfide during $SO_4$ reduction (Canfield, 1989; Canfield et al., 1992) and creates amorphous iron sulfide minerals, precursors to pyrite (Berner, 1970; Rickard, 1974; Yao and Millero, 1996). Concentrations of solid Fe phases other than pyrite were not measured at ODP sites 1030 and 1031. We modeled Fe(OH)$_3$(s) and FeS$_{am}$ as the representative phases and chose seafloor concentrations of 0.004 m$^3$/m$^3$ for Fe(OH)$_3$(s) $(\sim 120$ μmol/cm$^3$ sediment, similar to concentrations of reactive Fe-oxides measured in Mississippi delta sediments; Canfield, 1989) and 0 m$^3$/m$^3$ for FeS$_{am}$. We used a rate law for reductive dissolution of Fe(OH)$_3$(s) that includes a far-from-equilibrium dependence on Fe$_{am}^{3+}$ (Yao and Millero, 1996). Because we used a rate constant for FeS$_{am}$ high enough to maintain equilibrium with dissolved Fe$^{2+}$ and $H_2S$, the rate of reduction of Fe(OH)$_3$(s) controls the rate of formation of Fe$_{am}^{2+}$. This control is consistent with the experimental work of Rickard (1974), which indicated that the rate-controlling step in formation of FeS$_{am}$ from sulfidation of goethite is the dissolution of goethite. We did not model the formation of pyrite from FeS$_{am}$ and native sulfur (produced by reduction of Fe(OH)$_3$(s)), because this reaction does not have a substantial effect on pore-water solute concentrations.

3.2.5. SiO$_2$(s)\n
Measured pore-water silica concentrations, which are too high to be in equilibrium with the abundant quartz, feldspars, or clays (e.g., Mackenzie and Garrels, 1965), indicate that dissolution of SiO$_2$(am) controls the pore-water silica concentration at ODP Sites 1030 and 1031, as it does in most marine sediment (Fanning and Schink, 1969). Although the SiO$_2$(am) content was not measured, radiolarians, diatoms, and sponge spicules were noted in smear slides (Davis et al., 1997). The SiO$_2$(am) concentration in the surface sediments is probably $\sim 1$ wt%, similar to that measured in nearby Middle Valley sediments (Wheat and Tribble, 1994) and to that of other sediments underlying low-productivity surface waters (Fanning and Schink, 1969).

We used temperature-dependent solubility constants measured on biogenic silica from a siliceous ooze (Van Cappellen and Qui, 1997a), a rate law that includes a linear dependence on saturation state, as appropriate for moderately undersaturated fluids (Van Cappellen and Qui, 1997b), and a rate constant measured in aluminum-rich siliceous ooze (Rabouille et al., 1997; Van Cappellen and Qui, 1997b).

3.2.6. Ion Exchange and Surface Complexation

In environments where sedimentation rates are high or steady-state pore-water profiles have not developed (e.g., Reimers et al., 1996), adsorption of ions to mineral surfaces can influence pore-water solute concentrations. To test the importance of equilibrium-controlled sorption reactions at ODP sites 1030 and 1031, we ran simulations that included ion exchange (involving Na$^+$, Mg$^{2+}$, Ca$^{2+}$, K$^+$) on surface complexation (e.g., Dzombak and Morel, 1990; Stumm, 1992) of cations (H$^+$, Ca$^{2+}$, Mg$^{2+}$, Mn$^{2+}$, Fe$^{2+}$) and anions (PO$_4^{3-}$, SO$_4^{2-}$, CO$_3^{2-}$, $F^-$, $H_2BO_3^{-}$) on Fe(OH)$_3$(s). We based ion exchange parameters on the cation exchange capacity (15.8 meq/100 g sediment) and equivalent fractions of exchangeable cations ([equivalents adsorbed ion]/[total equivalents adsorbed ions]) measured in surface sediment from ODP site 1030 (Inoue, 2000). We calculated ion exchange equilibrium constants (Table 6) from the measured equivalent fractions of exchangeable cations and the activities of the ions that resulted from specification of the seawater boundary condition in Table 2 at 25°C. This calculation was made with the assumption that the activity of an absorbed cation is equal to its equivalent fraction (the Gaines-Thomas reaction; Appelo and Postma, 1993).

We modeled surface complexation involving “weak” and “strong” sites by means of equilibrium constants for 25°C (Table 7) and a double-layer model to calculate electrostatic corrections as a function of surface charge and pore-water ionic strength (Dzombak and Morel, 1990; Parkhurst, 1995). We used a value of 100 m$^2$/g for the specific surface area of Fe(OH)$_3$(s) (Yao and Millero, 1996) and site densities of 2.9 $\times$ 10$^{-6}$ and 7.3 $\times$ 10$^{-6}$ moles surface hydroxyls per m$^2$ mineral for the weak and strong sites, respectively (on the basis of values in Dzombak and Morel, 1990). The amount of each ion complexed to the solid phase at any depth depends on both pore-water composition and the concentration of Fe(OH)$_3$(s).

### Table 6. Cation exchange constants.a

<table>
<thead>
<tr>
<th>Exchange reaction</th>
<th>log $K$</th>
</tr>
</thead>
<tbody>
<tr>
<td>NaX = Na$^+$ + X$^-$</td>
<td>−1.31</td>
</tr>
<tr>
<td>KX = K$^+$ + X$^-$</td>
<td>−2.63</td>
</tr>
<tr>
<td>MgX$_2$ = Mg$^{2+}$ + 2X$^-$</td>
<td>−1.81</td>
</tr>
</tbody>
</table>

a Calculated from equivalent fractions measured by Inoue (2000).

b X represents a single exchange site.

### Table 7. Surface complexation constants at 25°C.

<table>
<thead>
<tr>
<th>Complexation reaction</th>
<th>log $K$</th>
</tr>
</thead>
<tbody>
<tr>
<td>∆H$^0$ + $H^+$ = ∆FeOH</td>
<td>8.93</td>
</tr>
<tr>
<td>∆FeOH$^2+$ = 2FeOH + $H^+$</td>
<td>−7.29</td>
</tr>
<tr>
<td>∆FeOCa$^2+$ + $H^+$ = ∆FeOH + Ca$^{2+}$</td>
<td>5.85</td>
</tr>
<tr>
<td>∆FeOMg$^2+$ + $H^+$ = ∆FeOH + Mg$^{2+}$</td>
<td>4.6</td>
</tr>
<tr>
<td>∆FeOMn$^2+$ + $H^+$ = ∆FeOH + Mn$^{2+}$</td>
<td>3.5</td>
</tr>
<tr>
<td>∆FeOF$^-$ + $H^+$ = ∆FeOH + Fe$^{2+}$</td>
<td>2.5</td>
</tr>
<tr>
<td>∆FeHPO$_4$ + $H_2O$ = ∆FeOH + PO$_4^{3-}$ + 3$H^+$</td>
<td>−31.29</td>
</tr>
<tr>
<td>∆FeHPO$_4$ + $H_2O$ = ∆FeOH + PO$_4^{3-}$ + 2$H^+$</td>
<td>−25.39</td>
</tr>
<tr>
<td>∆FePO$_4$ + $H_2O$ = ∆FeOH + PO$_4^{3-}$ + 3$H^+$</td>
<td>−17.72</td>
</tr>
<tr>
<td>∆FeSO$_4$ + $H_2O$ = ∆FeOH + SO$_4^{2-}$ + $H^+$</td>
<td>−7.78</td>
</tr>
<tr>
<td>∆FeHCO$_3$ + $H_2O$ = ∆FeOH + CO$_3^{2-}$</td>
<td>−0.79</td>
</tr>
<tr>
<td>∆FeHBO$_3$ + $H_2O$ = ∆FeOH + B(OH)$_3$(aq)</td>
<td>−0.62</td>
</tr>
<tr>
<td>∆Fe$^3+$ + $H_2O$ = ∆FeOH + $F^-$ + $H^+$</td>
<td>−8.7</td>
</tr>
<tr>
<td>∆Fe$^4+$ = 2FeOH + $F^-$</td>
<td>−1.6</td>
</tr>
<tr>
<td>∆FeCo$^3+$ + $H_2O$ = ∆FeOH + CO$_3^{2-}$ + $H^+$</td>
<td>−12.56</td>
</tr>
<tr>
<td>∆FeHCO$_3$ + $H_2O$ = ∆FeOH + CO$_3^{2-}$ + 2$H^+$</td>
<td>−20.62</td>
</tr>
</tbody>
</table>

thickness through which the solid phase was advected downward. Modeling sediment burial in this way was necessary to obtain the steady-state distribution of reactive solid phases. Because solute transport in the fluid phase occurred at least 20 times faster than sediment burial in all simulations (on the basis of the diffusion length scale), the simulations should provide a good indication of the chemical processes resulting from hydrothermal seepage, despite the inaccurate representation of sediment accumulation.

3.4. Parameter Estimation

To fit calculated profiles to measured pore-water concentrations, it was necessary to estimate (1) specific discharge, (2) concentration of reactive organic material entering the model domain, (3) the rate constant for \( \text{SO}_4 \) reduction, and (4) the reactive surface areas of \( \text{SiO}_2 \) and \( \text{Fe(OH)}_3 \). We estimated the first three of these with the nonlinear parameter estimation program PEST (Doherty et al., 1994), which minimizes the least squares error between calculated and measured values by varying the input to and repeatedly calling the forward simulation of ODP site 1030. The largest change was to calcite, CARFAP, and FeS (am) throughout the sediment column. They remained below 1.9 wt% dry at ODP sites 1030 and 1031, Davis et al., 1997, then estimated specific discharge by fitting calculated to measured pore-water Mg, which we assume behaves conservatively within the sediment section. We used the resulting specific discharge values for the remainder of the simulations. We next used pore-water \( \text{SO}_4 \) and \( \text{NH}_4 \) to estimate the concentration of reactive organic matter entering the model domain and the rate constant for \( \text{SO}_4 \) reduction. Finally, we adjusted the rate of \( \text{SiO}_2 \) dissolution by varying its reactive surface area until calculated \( \text{SO}_4 \) approximated the data and similarly adjusted the rate of \( \text{Fe(OH)}_3 \) dissolution. We did not use the model to constrain any reaction parameters associated with calcite, CARFAP, or FeS (am) because these minerals were essentially in equilibrium with pore fluids in all simulations.

4. MODEL RESULTS

Calculated total concentrations of Mg and of species involved in modeled diagenetic reactions are compared with measured values in Figure 2. Not shown is \( T_{\text{H}_2\text{SO}_4} \), which remained below \( -4 \times 10^{-6} \text{ mol/kg} \) in all simulations. Calculated pore fluid compositions are in equilibrium with calcite, CARFAP, and FeS (am) throughout the sediment column. They are undersaturated with both Fe(\( \text{OH} \)) 3 and SiO2 (am). Precipitation and dissolution of minerals resulted in small changes to mineral concentrations. The smallest change was to CARFAP concentration, +0.007 volume % (~0.03 wt% dry) in the simulation of ODP site 1030. The largest change was to calcite concentration, +0.5 volume % (~1.9 wt% dry) in the simulation of ODP site 1030.

The inclusion of \( \text{O}_2 \) respiration created a 15 cm deep seaflooroxic zone within which calculated pH, alkalinity, and \( T_{\text{PO}_4} \) were affected. Slightly elevated concentrations of alkalinity and \( T_{\text{PO}_4} \) persisted to ~10 mbsf in simulations that included \( \text{O}_2 \) respiration. Because we did not include inorganic N redox reactions or denitrification in the model reaction network, \( \text{O}_2 \) respiration did not affect \( T_{\text{NH}_4} \).

Because of the slow sedimentation rate, the inclusion of multicomponent ion exchange had no effect on calculated steady-state pore-water profiles despite the substantial cation mass incorporated into exchange sites.

The inclusion of surface complexation had a negligible effect on calculated pH. It affected calculated concentrations of solutes and alkalinity on a micromolar scale and thus influenced concentrations of solutes present at the lowest concentrations most significantly. In particular, surface complexation resulted in higher \( T_{\text{PO}_4} \) (by ~0.5 \( \mu \text{m} \)) and lower \( T_{\text{Fe}} \) (by ~2 \( \mu \text{m} \)) throughout most of the sediment column, as a result of desorption of \( \text{PO}_4 \) from sites in equilibrium with seawater within the upper few centimeters of the model domain. Desorption of \( \text{PO}_4 \) drove precipitation of CARFAP, which lowered the concentration of Fe. Because we do not have data to constrain processes occurring at depths <1 mbsf, we do not consider surface complexation reactions in the remaining discussion.

Calculated profiles for both sites provide a good match to measured Mg, \( \text{Ca}, \text{SO}_4 \), \( \text{NH}_4 \), and SiO2 (am) data and thus support the overall modeled reaction network and the use of a steady-state model to approximate the system. Discrepancies between calculated and measured concentrations of alkalinity and \( \text{PO}_4 \) at ODP site 1030, F at ODP site 1031, and pH and Fe at both sites suggest either that the reaction network used is incomplete or inaccurate in detail, or that the data are affected by sampling artifacts. These discrepancies are discussed further in section 4.2.

4.1. Model-Constrained Parameters

4.1.1. Specific Discharge

Best-fit specific discharge is 1.9 mm/yr at ODP site 1030 and 3.2 mm/yr at ODP site 1031. PEST returns 95% confidence intervals on the basis of the assumption that the relationship between model output (i.e., Mg concentrations) and parameter value (i.e., specific discharge) is linear (Doherty et al., 1994). Subject to this assumption and other assumptions described in Section 3, the upper and lower limits for specific discharge at ODP site 1030 are 2.0 mm/yr and 1.7 mm/yr, respectively. Those for specific discharge at ODP site 1031 are 3.6 mm/yr and 2.8 mm/yr, respectively.

4.1.2. Organic Matter Concentrations and Rate Constants

Best-fit rate constants for \( \text{SO}_4 \) reduction are \( 10^{-12.86} \text{ s}^{-1} \) and \( 10^{-13.00} \text{ s}^{-1} \) at ODP sites 1030 and 1031, respectively (Table 3). The constants are consistent with those predicted on the basis of sedimentation rate (Toth and Lerman, 1977). Depth-integrated rates of \( \text{SO}_4 \) reduction (8.2 \( \times 10^{-3} \) and 3.3 \( \times 10^{-3} \) mol \( \text{SO}_4 /\text{m}^2/\text{yr} \) at ODP sites 1030 and 1031, respectively) are consistent with rates calculated for other deep-sea sediments near continental margins (Canfield, 1991).

Model-constrained concentrations of organic carbon entering the top of the model domain represent concentrations entering the \( \text{SO}_4 \) reduction zone, not seafloor concentrations. Best-fit concentrations are 268 mol C/m3 bulk and 160 mol C/m3 bulk at ODP sites 1030 and 1031, respectively, and are similar to total organic carbon concentrations measured in sediments from depths up to 40 mbsf at ODP site 1031 (130 to 290 mol C/m3 bulk; Davis et al., 1997). They are 16 to 30 times less than the seafloor concentration predicted on the basis of sedimentation rate (Tromp et al., 1995) and 5 to 9 times less than the constant concentration chosen by Ingall and Van Cappellen (1990) as representative of most of the seafloor. These comparisons suggest that 80 to 95% of the reactive organic matter reaching the seafloor at ODP sites 1030 and 1031 is consumed by degradation pathways other than \( \text{SO}_4 \) reduction.

The rate constant for \( \text{SO}_4 \) reduction and the organic carbon concentration entering the \( \text{SO}_4 \) reduction zone are better con-
strained for ODP site 1030 than for ODP site 1031. We used the 95% confidence intervals determined for ODP site 1030 (log $k = -12.95$ to $-12.78$ and organic carbon concentration $= 254$ to 283 mol C/m$^3$ bulk) to assess the influence of small changes in these parameters on seafloor solute fluxes (Section 5).

4.1.3. Reactive Surface Areas

Model-constrained reactive surface areas ($2 \times 10^{-5}$ m$^2$/g for both Fe(OH)$_3$(s) and SiO$_2$(am)) are $10^6$ to $10^7$ times smaller than physical surface areas assumed or measured in experimental studies (Yao and Millero, 1996; Van Cappellen and Qiu, 1997b). Several possible reasons for these differences exist. (1) The rate constants we used were measured on synthetic Fe(OH)$_3$(s) and on SiO$_2$(am) from surface sediments. The aged, in situ phases may be less reactive because of a combination of adsorption of ions and smoothing of surface defects by recrystallization over time (Yao and Millero, 1996; Rabouille et al., 1997; Van Cappellen and Qiu, 1997b). (2) We used solubility and rate constants measured on SiO$_2$(am) from a siliceous ooze. In the aluminum-rich sediments at ODP sites 1030 and 1031, adsorption of aluminum may decrease both the solubility and the reactivity of SiO$_2$(am) and/or authigenic (amorphous) aluminosilicates may control silica solubility (Rabouille et al., 1997; Van Cappellen and Qiu, 1997a, 1997b; Dixit et al., 2001). (3) The solubility of iron may be affected by the formation of unaccounted for authigenic phases, or the dissolving iron phase might be an Fe(III)-(hydr)oxide that is less reactive than Fe(OH)$_3$(am), such as goethite or hematite (Canfield et al., 1992).

4.2. Model Discrepancies

Discrepancies between measured and calculated pore-water profiles resulted for species whose concentrations are affected by multiple processes both in situ and during sampling. For the upper 20 m of ODP site 1030, calculated alkalinity and $T_{PO_4}$ are higher than measured values (by $\sim 1$ meq/kg and $\sim 1$ μmol/kg, respectively), and calculated pH is lower (by $\sim 0.7$ log units). For ODP sites 1030 and 1031, calculated $T_{Fe(II)}$ is larger than the measured concentration of Fe.

4.2.1. In Situ Processes

One possible explanation for discrepancies between calculated and measured pH, alkalinity, and $PO_4$ is that our model of the processes occurring in the sediment column is lacking an in situ reaction capable of buffering pH at higher values. Such a reaction would lower calculated alkalinity and $T_{PO_4}$ through enhanced calcite and CARFAP precipitation. A simulation of ODP site 1030 in which pH was held at 7.6 (approximately equal to the measured pH) throughout the model domain resulted in alkalinity and $T_{PO_4}$ lower than measured (Fig. 3). Increasing the rate of reductive dissolution of Fe(OH)$_3$(s) (e.g., Boudreau and Canfield, 1993) to the point at which siderite (FeCO$_3$) precipitation buffers $T_{Fe(II)}$ at 40 times measured values increased pH only modestly, but did result in calculated alkalinity and $T_{PO_4}$ in the top 20 m of the model domain that more closely match measured values (Fig. 4). We considered dissolution and precipitation of several silicate minerals, although our ability to model such reactions was limited by the lack of dissolved Al data. When reactions involving plagioclase, potassium feldspar, illite, saponite, and sepiolite produced reasonable fits to dissolved SiO$_2$, Ca, K, and Mg data, the reactions had negligible effect on pH.

4.2.2. Potential Sampling Artifacts

Alternatively, changes in pressure and redox environment associated with core retrieval and sampling may have resulted in experimental artifacts. Alkalinity in pore-water samples collected onboard ship is commonly tens to hundreds of milliequivalents per kilogram less than that of samples collected in situ because of precipi-
tation of calcite during core retrieval (e.g., Murray et al., 1980; Emerson et al., 1982). Calcite precipitation would cause pH to drop (e.g., Murray et al., 1980), but degassing of CO₂ would cause pH to increase during core retrieval. We simulated the equilibration of calculated alkalinity and pH with calcite and the partial pressure of atmospheric CO₂ (3.5 × 10⁻⁴ atm) at atmospheric pressure and laboratory temperature (18°C) (Fig. 5). Reequilibration of calculated curves with calcite without degassing CO₂ produced alkalinity values very close to measured values. Reequilibration of calculated curves with calcite and complete degassing of CO₂ produced pH very close to measured pH. Some combination of partial equilibration of pore water with calcite and partial degassing of CO₂ may explain the offset between calculated and measured values.

Sampling of anoxic pore waters in the presence of O₂ can cause oxidation of dissolved Fe(II) and precipitation of Fe(III)-(hydr)oxides (Troup et al., 1974; Loder et al., 1978). In experiments documenting this process as much as 50 to 75% of dissolved Fe precipitated (Troup et al., 1974; Loder et al., 1978).

Phosphate deficits of 1 to 3 μmol/kg have been attributed to the decrease in pressure during core retrieval, but the mechanism by which PO₄ is removed from solution is not known (Jahnke et al., 1982, 1989). Because PO₄ adsorbs to both calcite (Avnimelech, 1980) and Fe(III)-(hydr)oxides (Bray et al., 1973), precipitation of either could result in PO₄ removal.

Because sampling artifacts likely affect measured concentrations of several species and no obvious in situ process accounts for differences between calculated and measured profiles, we assume that calculated pore-water concentrations represent in situ values for all species in subsequent flux calculations.

Fig. 5. Equilibration of ODP site 1030 calculated (a) pH and (b) alkalinity at surface temperature and pressure with calcite alone (dotted lines) and with calcite and the partial pressure of atmospheric CO₂ (dashed lines). Other symbols as in Figure 2.

5. SOLUTE FLUXES

5.1. Definitions

To assess how reaction within the sediment column affects solute fluxes, we compared model-derived “sediment hydrothermal fluxes” to “basement hydrothermal fluxes.” We defined the sediment hydrothermal flux (Fₛ) of a species as the difference between the “seepage flux” (Fₛ) and the net seafloor flux resulting from coupled diagenesis and upward seepage of basement fluid (Table 2). The “diagenetic flux” (F₅) is the net seafloor flux across the seafloor resulting from diagenesis in the absence of flow:

\[ F_S = F_S - F_D. \]  

We defined the basement hydrothermal flux (Fᵥ) of a species as the net advective flux that would result from pipelike flow of basement fluid into the ocean:

\[ F_B = q (T_{bw} - T_{sw}). \]

where q is specific discharge, Tₚ is the total concentration of a primary species in basement fluid, and Tₚ is its total concentration in seawater (Table 2). Flux definitions are schematically illustrated in Figure 6. All fluxes are total fluxes of primary species (analogous to total concentrations). A flux <0
is a flux into the sediment (a sink); a flux >0 is a flux to the ocean (a source).

We quantified the importance of reaction within the sediment column to hydrothermal fluxes of solutes by taking the ratio of sediment hydrothermal flux to basement hydrothermal flux (FSH/FB). If reaction within the sediment section increases the magnitude of a flux without changing its direction then FSH/FB > 1. If it reverses the direction of a flux (sink becomes a source or vice versa), then FSH/FB < 0.

Coupling upward advection of hydrothermal fluid with sediment diagenesis can create sediment hydrothermal fluxes that differ from basement hydrothermal fluxes in two ways (Fig. 6). First, upward advection increases the size of seafloor concentration gradients and therefore of diffusive fluxes at the seafloor (Fig. 6c). This phenomenon affects fluxes of all species. Second, because upward advection changes the distribution of solutes, rates of mineral precipitation and dissolution that depend on solute concentration change. For aqueous species involved in these reactions, the total (depth-integrated) rate of production in the sediment section in the presence of seepage (Rg) differs from that resulting from diagenesis alone (Rg), (Fig. 6d).

5.2. Dependence on Flow Rate

5.2.1. Slow Flow: Net Fluxes at ODP sites 1030 and 1031

At ODP sites 1030 and 1031 basement fluid is enriched relative to seawater in NH4, SiO2, and Ca, and depleted in SO4, PO4, and alkalinity (Table 2). The basement hydrothermal system is therefore a source of NH4, SiO2, and Ca and a sink of SO4, PO4, and alkalinity. Reaction of upwelling fluid within the sediment section does not reverse the sense of any of these fluxes, but does change the magnitude of all of them (Table 8). Sediment hydrothermal sources of NH4 and SiO2 are larger than basement hydrothermal sources (FSH/FB = 2.6 and 12, respectively, at ODP site 1030), and sediment hydrothermal sinks of SO4 and PO4 are larger than basement hydrothermal sinks (FSH/FB = 1.2 and 1.9, respectively, at ODP site 1030). Reaction within the sediment decreases the hydrothermal source of Ca (FSH/FB = 0.9). It has a variable effect on the hydrothermal sink of alkalinity. At ODP site 1031, the sediment hydrothermal sink of alkalinity is larger than the basement hydrothermal sink (FSH/FB = 1.6), but at ODP site 1030 it is smaller (FSH/FB = 0.8).

Variation of the rate constant for SO4 reduction and of the concentration of organic carbon entering the model domain within the 95% confidence intervals calculated for ODP site 1030 (± ~20% and ± ~5%, respectively) altered flux ratios by a few percent or less (Table 9). Alkalinity was the most sensitive to these parameters with flux ratios altered by ~10%.

Sediment hydrothermal fluxes of SO4 and NH4 differ from basement hydrothermal fluxes solely because of the increased seafloor concentration gradients caused by seepage. Seepage does not alter depth-integrated reaction rates of SO4 and NH4 (Rg = Rg), (Table 8), because the rate of organic matter degradation has a negligible dependence on fluid composition (Eqn. 2). Sediment hydrothermal fluxes of SiO2, PO4, and alkalinity differ from basement hydrothermal fluxes as a result of

<table>
<thead>
<tr>
<th>Species</th>
<th>FB (mol/ m2/yr)</th>
<th>FSH (mol/ m2/yr)</th>
<th>FSH/FB</th>
<th>RF (mol/ m2/yr)</th>
<th>RS (mol/ m2/yr)</th>
</tr>
</thead>
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<tr>
<td>SO4</td>
<td>1.17E-02</td>
<td>7.8E-03</td>
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<td>3.1E-02</td>
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<tr>
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<td>1.7E-02</td>
<td>3.4E-02</td>
<td>2.6E-02</td>
<td>2.6E-02</td>
</tr>
<tr>
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<td>3.9E-02</td>
<td>2.9E-02</td>
<td>2.9E-02</td>
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<tr>
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<td>2.7E-02</td>
<td>7.0E-02</td>
<td>1.3E-02</td>
</tr>
<tr>
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<td>3.5E-02</td>
<td>7.0E-02</td>
<td>1.4E-02</td>
</tr>
<tr>
<td>Alkalinity</td>
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<td>5.9E-04</td>
<td>3.0E-03</td>
<td>5.0E-04</td>
<td>1.1E-02</td>
</tr>
</tbody>
</table>

a A flux >0 indicates a source to the ocean. A rate >0 indicates net production of a solute within the sediment column.

Table 9. Sensitivity of FSH/FB to SO4 reduction rate.

<table>
<thead>
<tr>
<th>Species</th>
<th>Lowa</th>
<th>Highb</th>
<th>Lowc</th>
<th>Highd</th>
</tr>
</thead>
<tbody>
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<td>1.2</td>
<td>1.1</td>
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<td>2.8</td>
<td>2.7</td>
<td>2.5</td>
</tr>
<tr>
<td>SiO2</td>
<td>12.8</td>
<td>12.0</td>
<td>12.3</td>
<td>12.4</td>
</tr>
<tr>
<td>Ca</td>
<td>0.9</td>
<td>0.9</td>
<td>0.9</td>
<td>0.9</td>
</tr>
<tr>
<td>PO4</td>
<td>2.0</td>
<td>1.8</td>
<td>1.9</td>
<td>1.9</td>
</tr>
<tr>
<td>Alkalinity</td>
<td>0.9</td>
<td>0.7</td>
<td>0.8</td>
<td>0.9</td>
</tr>
</tbody>
</table>

a log k = -12.95.
b log k = -12.78.
c 254 mol C/ m2 bulk.
d 283 mol C/ m2 bulk.
differences in depth-integrated reaction rates with and without seepage ($R_S \neq R_D$; Table 8). Seepage increases the rate of SiO$_2$(am) dissolution and of CARFAP precipitation. At ODP site 1031 seepage increases the rate of calcite precipitation, but at ODP site 1030 seepage decreases the rate of calcite precipitation. Despite having opposite effects on calcite precipitation rate at the two sites, upward seepage of fluid has the same effect on hydrothermal fluxes of Ca at both sites, because diagenetic fluxes of Ca are small relative to hydrothermal fluxes (Table 8).

5.2.2. Faster Flow

We simulated specific discharge of 1 to 100 mm/yr through a sediment column having all other characteristics identical to ODP site 1030. Rates of upward seepage estimated in ridge flank (crust older than 1 My) settings are typically at the lower end of this range (e.g., Mottl, 1989; Wheat and Mottl, 1994). Faster rates of upward seepage through sediment have been documented on very young crust (<1 My) (e.g., Maris and Bender, 1982; Wheat and McDuff, 1995).

With increasing specific discharge (and increasing basement hydrothermal flux), the relative contribution of reaction within the sediment section to hydrothermal fluxes of SO$_4$, NH$_4$, and SiO$_2$(aq) decreased (Fig. 7), because these species have constant rates of production (NH$_4$ and SiO$_2$(aq)) and consumption (SO$_4$) within the sediment column ($R_S$ is approximately equal to the difference between $F_S$ and $F_B$ in Fig. 7). The contribution of sediment reaction became relatively unimportant to fluxes of

Fig. 7. Net seafloor fluxes resulting from ODP site 1030 parameters as a function of specific discharge. (a) SO$_4$, (b) NH$_4$, (c) SiO$_2$(aq), (d) alkalinity, (e) PO$_4$, (f) Ca. Upper plot of each pair: $F_S$ (solid line), $F_B$ (dashed line), and $F_{SH}$ (dotted line) obtained in simulations that did not include O$_2$ respiration. ($F_B = F_S$ at 0 mm/yr specific discharge.) Lower plot of each pair: $F_{SH}/F_B$ obtained in simulations that did not include O$_2$ respiration (solid circles) and in simulations that included O$_2$ respiration (open circles in plots of PO$_4$ and alkalinity fluxes). Horizontal dotted line plots at $F_{SH}/F_B = 1$. 
SO\textsubscript{4} and NH\textsubscript{4} at slow to moderate flow rates (\(F_{\text{sed}}/F_b < 1.1\) at specific discharge >5 mm/yr and \(F_{\text{sed}}/F_b < 1.1\) at specific discharge >20 mm/yr, respectively). Sediment reaction remained an important hydrothermal source of SiO\textsubscript{2(aq)} over the range of simulated flow rates (\(F_{\text{sed}}/F_b = 1.5\) at specific discharge = 100 mm/yr). Extrapolation of the SiO\textsubscript{2(aq)} fluxes to greater flow rates suggests that the sediment contribution to the hydrothermal flux would remain relatively important (\(F_{\text{sed}}/F_b > 1.1\)) up to flow rates of <500 mm/yr. The extrapolation may not be valid, however, because the assumption of a linear thermal gradient is not valid for specific discharge >300 mm/yr.

Increasing specific discharge decreased the importance of sediment reaction to hydrothermal fluxes of Ca. At a specific discharge of 100 mm/yr, the sediment hydrothermal flux of Ca differed from the basement hydrothermal flux by <1%.

Increasing specific discharge up to 100 mm/yr had little effect on the relative importance of the sediment column to hydrothermal fluxes of PO\textsubscript{4} (\(F_{\text{sed}}/F_b \sim 2.0\)) and to hydrothermal fluxes of alkalinity at specific discharge \(\geqslant 5\) mm/yr (\(F_{\text{sed}}/F_b \sim 1.5\)). Rate constants for CARFAP and calcite precipitation are high enough to maintain local equilibrium between pore fluids and these minerals. Because the resulting transport-controlled rates of precipitation \((R_p)\) increased with increasing specific discharge, sediment hydrothermal sinks increased more rapidly than basement hydrothermal sinks (Figs. 7d,e). Including O\textsubscript{2} respiration in the simulations resulted in larger sediment hydrothermal sinks of PO\textsubscript{4} and alkalinity at all flow rates.

### 5.3. Dependence on Sediment Thickness

By use of parameters appropriate for ODP site 1030 and specific discharge of 1.9 and 10 mm/yr, we calculated fluxes through sediment 10 to 100 m thick. Flow rates of 1 to 2 mm/yr have been estimated in areas with as much as 200 m of sediment cover (Mottl, 1989). Flow rates of tens of millimeters per year have only been documented where sediment thickness is less than 50 m (e.g., Maris and Bender, 1982; Wheat and McDuff, 1995).

Over a range of sediment thickness, the sediment hydrothermal flux of a species varies if the size of either the seepage flux or the diagenetic flux varies with sediment thickness (Eqn. 10). Both seepage fluxes and diagenetic fluxes changed with increasing sediment thickness (Fig. 8, upper plots) as a result of increased quantities of reactive solid phases (i.e., organic matter and SiO\textsubscript{2(aq)}). Because the boundary condition concentrations and temperatures did not change with sediment thickness, decreasing concentration and temperature gradients drove additional changes in diagenetic fluxes. For instance, the sediment hydrothermal source of Ca increased with increasing sediment thickness (\(F_{\text{sed}}/F_b\) approached 1) because the diagenetic source of Ca decreased as the distance between the sea floor and the sediment–basement interface increased. For all solutes a faster flow rate (10 mm/yr) decreased the influence of sediment thickness on the relative contribution of the sediment section to hydrothermal fluxes (Fig. 8, lower plots).

For SO\textsubscript{4}, NH\textsubscript{4}, PO\textsubscript{4}, and alkalinity, the response of the sediment hydrothermal flux to sediment thickness was controlled by the length of the SO\textsubscript{4} reduction zone, which reached a maximum of ~47 m in these models. A sediment thickness of 40 to 47 m resulted in maximum ratios of \(F_{\text{sed}}/F_b\) for SO\textsubscript{4} (1.2) and NH\textsubscript{4} (2.6), a minimum ratio for alkalinity (0.8), and an inflection point in the plot of \(F_{\text{sed}}/F_b\) for PO\textsubscript{4} (Fig. 8, lower plots). As sediment thickness increased beyond 47 m, seepage fluxes of SO\textsubscript{4} and NH\textsubscript{4} changed little (Figs. 8a,b, upper plots), and diagenetic fluxes responded to the increasing distance (and decreasing concentration gradients) between the SO\textsubscript{4} reduction zone and the base of the sediment column. Because the diagenetic sink of SO\textsubscript{4} and source of NH\textsubscript{4} increased, the sediment hydrothermal sink and source decreased. With increasing sediment thickness, lower temperatures within the SO\textsubscript{4} reduction zone caused the diagenetic sources of PO\textsubscript{4} and alkalinity to increase as a result of reduced rates of CARFAP and calcite precipitation (Figs. 8d,e, upper plots). The larger diagenetic sources resulted in larger sediment hydrothermal sinks of PO\textsubscript{4} and alkalinity (\(F_{\text{sed}}/F_b = 2.4\) and 1.1, respectively, at a sediment thickness of 100 m).

The depth at which organic matter ran out in these simulations is coincident with the length of the sediment column at ODP site 1030, because we set the bottom boundary condition concentrations of SO\textsubscript{4} and NH\textsubscript{4} equal to the concentrations in the deepest pore fluid sample, taken at a depth 5 m above the base of the sediment column. In general, sediment hydrothermal fluxes of SO\textsubscript{4} and NH\textsubscript{4} will be maximized when the length of the sediment column equals the maximum possible length of the SO\textsubscript{4} reduction zone. A larger concentration of organic matter or a slower rate constant for SO\textsubscript{4} reduction would result in maximum sediment hydrothermal fluxes at greater sediment thickness.

The relative importance of the sediment section to hydrothermal fluxes of SiO\textsubscript{2(aq)} increased with increasing sediment thickness (at a sediment thickness of 100 m, \(F_{\text{sed}}/F_b = 30\)), due primarily to differences in the distribution of SiO\textsubscript{2(aq)} with and without flow. Warm temperatures caused faster SiO\textsubscript{2(aq)} dissolution at the base of the sediment column than at the top. Without flow, most of the SiO\textsubscript{2(aq)} thus produced diffused out of the sediment section across the bottom boundary. With flow it exited across the seafloor. Because SiO\textsubscript{2(aq)} persisted to the base of the sediment column over the simulated range of sediment thickness, a thicker sediment column increased the depth-integrated production rate of SiO\textsubscript{2(aq)} and amplified the effect of fluid flow.

### 5.4. Global Implications

If a portion of the hydrothermal fluid escaping basement at warm ridge-flank seepage sites passes through sediment, then global estimates of solute fluxes from warm sites need to account for changes in solute concentrations that occur within the sediment. To demonstrate the maximum effect sediment of the type found at ODP sites 1030 and 1031 could have on global fluxes of solutes from warm ridge-flank sites, we multiplied the global flux estimates derived from Baby Bare spring water (basement fluid) composition (Sansone et al., 1998; Wheat and Mottl, 2000) by the ratios of sediment hydrothermal to basement hydrothermal flux determined in this study. For a sediment thickness of 47 m and a specific discharge of 1.9 mm/yr this calculation results in larger fluxes of SO\textsubscript{4}, NH\textsubscript{4}, SiO\textsubscript{2(aq)}, and PO\textsubscript{4} and smaller fluxes of Ca and alkalinity (Table
For most species this choice of sediment thickness and specific discharge maximizes the percent difference between the estimate derived from basement fluid composition and the estimate that accounts for reaction within the sediment section. For alkalinity, sediments have a larger and opposite effect at faster flow rates; interaction with sediments (at specific discharge of 5 to 100 mm/yr) could increase the global flux of alkalinity from warm ridge-flank hydrothermal sites to as much as $10^{10}$ eq/yr. For PO$_4$ and SiO$_2$(aq) thicker sediments have a greater effect; interaction with sediments (100 m thick) could increase global fluxes of PO$_4$ and SiO$_2$(aq) to as much as $7 \times 10^8$ mol/yr and $5.4 \times 10^{11}$ mol/yr, respectively.

Differences between flux estimates that do and do not account for reaction within the sediment section are small in comparison to estimates of river input fluxes for all species except SiO$_2$(aq) (Table 1). Reaction within the sediment section could increase the source of SiO$_2$(aq) from <1% to as much as 11% of river input if interaction of warm hydrothermal fluids with thick (100 m) sediment were ubiquitous. The actual contribution of reaction within the sediment section to warm ridge-flank fluxes will be proportional to the fraction of upwelling hydrothermal fluid that passes through the sediment and must be less than our estimates if this sediment mineralogy and our choice of diagenetic reactions are representative of warm ridge-flank environments. Different sediment mineralogy or reactive organic carbon content would result in different estimates of sediment-influenced hydrothermal fluxes.

Fig. 8. Net seafloor fluxes resulting from ODP site 1030 parameters as a function of sediment thickness. (a) SO$_4$, (b) NH$_4$, (c) SiO$_2$(aq), (d) alkalinity, (e) PO$_4$, (f) Ca. Upper plot of each pair: $F_S$ (solid line), $F_B$ (dashed line), $F_D$ (dot-dash line), and $F_{SH}$ (dotted line) obtained in simulations with specific discharge $= 1.9$ mm/yr. Horizontal solid line plots at 0 mol/m$^2$/yr.

Lower plot of each pair: $F_{SH}/F_B$ obtained in simulations with specific discharge $= 1.9$ mm/yr (solid circles) and in simulations with specific discharge $= 10$ mm/yr (open circles). Horizontal dotted line plots at $F_{SH}/F_B = 1$.
6. SUMMARY AND CONCLUSIONS

Estimates of solute fluxes to and from the ocean associated with ridge-flank hydrothermal systems are usually made on the basis of basement pore fluid or mineral composition. We used pore-water geochemical data from ODP sites 1030 and 1031 on the eastern flank of the Juan de Fuca Ridge to examine the influence of reaction within the sediment column on hydrothermal fluxes of solutes at this site of upwelling hydrothermal fluid. We used the reactive-transport code GIMRT to model the processes occurring in the sediment column (including diagenesis, upward fluid flow, sediment burial, and molecular diffusion) and to estimate seafloor fluxes of Ca, SiO$_2$(aq), SO$_4$, PO$_4$, NH$_4$, and alkalinity. Calculated concentrations of solutes best matched measured concentrations with flow rates (specific discharge) of 1.9 mm/yr at ODP site 1030 and 3.2 mm/yr at ODP site 1031 and with the following diagenetic reactions included in the model: organic matter degradation via SO$_4$ reduction; rate-controlled dissolution of amorphous silica and of amorphous Fe(III)-(hydr)oxide; and (equilibrium) precipitation of calcite, carbonate fluorapatite, and amorphous Fe(II)-sulfide.

At ODP sites 1030 and 1031, basement fluid is enriched relative to seawater in NH$_4$, SiO$_2$, and Ca, and depleted in SO$_4$, PO$_4$, and alkalinity. The basement hydrothermal system therefore serves as a source of NH$_4$, SiO$_2$, and Ca and a sink of SO$_4$, PO$_4$, and alkalinity. Reaction of upwelling fluid within the sediment section does not reverse the sense of any of these fluxes, but does change the magnitude of all of them. Reaction within the sediment results in larger hydrothermal sources of NH$_4$ and SiO$_2$(aq), larger hydrothermal sinks of SO$_4$ and PO$_4$, and a smaller hydrothermal source of Ca than would result if basement fluid discharged directly to the ocean without interaction with the sediment section. At ODP site 1031, sediment reaction results in a larger hydrothermal sink of alkalinity, but at ODP site 1030 it results in a smaller sink.

Two series of simulations in which we varied fluid flow rate (1 to 100 mm/yr) and sediment thickness (10 to 100 m) predict that the sediment section will contribute most significantly to fluxes of SO$_4$ and NH$_4$ at slow flow rates and intermediate sediment thickness and to fluxes of SiO$_2$(aq) at slow flow rates and large sediment thickness. Reaction within the sediment section could approximately double the hydrothermal sink of PO$_4$ over a range of flow rates and sediment thickness and could slightly decrease (by \( \leq 10\% \)) the size of the hydrothermal source of Ca. Sediment reaction could increase or decrease the hydrothermal sink of alkalinity depending on both flow rate and sediment thickness.

Flux estimates are reliable to the extent that the modeled reaction network provides a reasonable description of the diagenetic processes affecting major ion concentrations within the sediment section. Some of the results reported here suggest that other diagenetic processes may influence hydrothermal fluxes in this and similar settings. Upwelling hydrothermal fluid in the O$_2$ respiration zone may create hydrothermal sinks of PO$_4$ and alkalinity in addition to those created in the SO$_4$ reduction zone. Surface complexation may affect PO$_4$ fluxes. The aluminum content of the sediment may affect the solubility and reactivity of SiO$_2$(am) (e.g., Dixit et al., 2001) and thus affect SiO$_2$(aq) fluxes.

Our results indicate that upward seepage of warm ridge-flank hydrothermal fluid through the sediment section can significantly increase or decrease local hydrothermal fluxes of solutes. On a global scale the effect of sediment reaction will depend on the fraction of fluid that passes through, rather than bypasses, the sediment. Even if all warm ridge-flank fluid were filtered through the sediment, the resulting increases and decreases in the global hydrothermal fluxes of the solutes considered in this study are likely to be small in comparison to the river input fluxes of these solutes. The sediment section potentially influences the flux of SiO$_2$(aq) the most. Reaction with sediment could increase this flux from \(<1\%\) to several percent of the river input flux.

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**APPENDIX**

**Formulation of Multicomponent Diffusion**

In multicomponent systems, interactions between species in solution result in rates of diffusion that differ from those predicted by Fick’s Law. Where nonideal interactions between species occur, gradients in chemical potential (which depends on the activity of a species), not concentration, drive diffusion. The charge imbalance that arises when charged species diffuse at differing rates drives an additional nonadvective flux known as electrochemical migration (Lichtner, 1979; Mc- Duff and Ellis, 1979; Newman, 1991; Lichtner, 1996; Van Cappellen and Gaillard, 1996). Diffusion driven by gradients in chemical potential and electrochemical migration are included in a general expression for nonadvective flux similar to that derived by Van Cappellen and Gail- lard (1996). The flux of an individual species is given by

\[ J_i = u_i^s C_i \left( -\nabla \mu_i + z_i F \right), \]  
(A1)

where \( u_i^s \) is the mobility of species \( i \), \( C_i \) its concentration, \( \mu_i \) its chemical potential, \( z_i \) its charge, \( F \) is Faraday’s constant (coulombs/mole), and \( E \), the electrical field, is equal to the gradient in electrical potential, \( \Phi \) (\( E = -\nabla \Phi \)). Because pore waters typically remain electrically neutral (there are no imposed currents), the sum of the charge fluxes is zero:

\[ \sum_{i=1}^{N_{tot}} z_i J_i = 0, \]  
(A2)

where \( N_{tot} \) is the total number of species in the system. Combining Eqs. A1 and A2, results in an expression for the electrical field in terms of chemical potential:

\[ E = -\nabla \Phi = \frac{\sum_{i=1}^{N_{tot}} z_i u_i^s C_i \nabla \mu_i}{F \sum_{i=1}^{N_{tot}} z_i u_i^s C_i}, \]  
(A3)

which is substituted into Eqn. A1 to obtain an expression for diffusion plus electrochemical migration that is written in terms of chemical potential (Van Cappellen and Gaillard, 1996):

\[ J_i = -u_i^s C_i \nabla \mu_i + u_i^s z_i C_i \sum_{j=1}^{N_{tot}} z_j u_j^s C_j \nabla \mu_j, \]  
(A4)

To obtain an expression for flux in terms of concentrations, the chemical potential is expanded to:

\[ \mu_i = \mu_i^0 + R T \ln(\gamma_i C_i), \]  
(A5)

where \( R \) is the ideal gas constant, \( T \) is temperature (Kelvin), and \( \gamma_i \) is the activity coefficient for species \( i \). The tracer diffusion coefficient is related to the mobility of the ion through the Nernst-Einstein relation (Lassaga, 1998):

\[ D_i^0 = u_i^s R T. \]  
(A6)

A general expression for the nonadvective flux of a solute \( i \) in terms of
concentrations and activity coefficients is obtained by differentiating Eqn. A5 and substituting the result and Eqn. A6 into Eqn. A4:

\[ J_i = -\left[ D_i \nabla C_i + D'_i \nabla \ln \gamma_i - D'_i \nabla C_i \right] \sum_{l=1}^{N_e} \frac{z_i z_l D_l \nabla C_l}{C_l} \frac{1}{\sum_{k=1}^{N_e} z_k D_k} \]. \tag{A7}

Gradients in ionic strength and temperature are small in the system we are considering, so we neglect the contribution to the flux from the gradients in the logarithms of the activity coefficients. With this approximation, the flux of an individual species becomes:

\[ J_i = -\left[ D_i \nabla C_i - D'_i \nabla C_i \right] \sum_{l=1}^{N_e} \frac{z_i z_l D_l \nabla C_l}{C_l} \frac{1}{\sum_{k=1}^{N_e} z_k D_k} \]. \tag{A8}

The total nonadvective flux of a primary species \( J^{\text{tot}}_i \) in Eqn. 2 is found by summing across the fluxes of the individual species contributing to the total concentration of the primary species (Lichtner, 1996):

\[ J^{\text{tot}}_i = J_i + \sum_{j=1}^{N_p} v_{ij} J_j. \tag{A9} \]

Substituting Eqn. A8 into Eqn. A9, and replacing the tracer diffusion coefficients with diffusion coefficients appropriate for the porous medium, one obtains:

\[ J^{\text{tot}}_i = -\left[ D^{\text{pm}} \nabla C_i + \sum_{j=1}^{N_p} v_{ij} D^{\text{pm}} \nabla C_i - T'_i \frac{1}{\sum_{j=1}^{N_p} z_j D^{\text{pm}}} \right] \sum_{l=1}^{N_e} \frac{z_i z_j D_c \nabla C_l}{C_l} \]. \tag{A10}

where the \( T' \) term is defined as

\[ T'_i = z_i D^{\text{pm}} C_j + \sum_{j=1}^{N_p} v_{ij} D^{\text{pm}} C_i. \tag{A11} \]

Eqn. A10 can be further transformed to the equation implemented in GIMRT by noting that reactions (including the ones linking primary and secondary species) must be electrically balanced, leading to a charge conservation equation for each reaction in the system (e.g., Lichtner, 1996). The charge conservation equation can be used to obtain the charge of the \( i \)th secondary species in terms of the charges of the primary species (Lichtner, 1996):

\[ z_i = \sum_{j=1}^{N_p} v_{ij} z_j, \tag{A12} \]

where \( N_p \) is the number of primary species in the system. Substituting this result into Eqn. A10 above, factoring primary species charges where appropriate, and noting that summation terms commute, one obtains:

\[ J^{\text{tot}}_i = -\left[ D^{\text{pm}} \nabla C_i + \sum_{j=1}^{N_p} v_{ij} D^{\text{pm}} \nabla C_i \right. \]

\[ \left. - T'_i \frac{1}{\sum_{j=1}^{N_p} z_j T'_j} \right] \sum_{j=1}^{N_p} \frac{z_i z_j D_c \nabla C_j}{C_j} \]. \tag{A13}

This is the equation implemented in GIMRT and the expression given by Lichtner (1996) (eqn. 284) except that the numerator of the last term on the right-hand side is summed over all of the \( l \) primary species. The last term on the right-hand side represents the contribution from electrochemical migration and ensures that electroneutrality in the solution is maintained.

When electrochemical migration is modeled, care must be taken to consider only charge-balanced solutions and charge-balanced reactions. A charge imbalanced solution in an initial or boundary condition would generate an unrealistic flux, as would a reaction that generated a net charge. Surface complexation reactions, if not modeled in conjunction with an explicit calculation of the diffuse layer composition, are such reactions. Charge balance is between the solution and the charged mineral surfaces. Because species in solution are mobile and surface species (except for burial) are not, a charge imbalance develops in solution as surface complexation reactions occur (Parkhurst, 1995; Lichtner, 1996). Modeling a diffuse layer that remains immobile and balances the charge on mineral surfaces would ensure that the mobile aqueous phase remains charge-balanced as surface complexation reactions proceed. Parkhurst (1995) presented such a formulation, but it has not been implemented here because of the high computational cost of the calculation.